



Model averaging to determine reaction process endpoint

**using infrared spectroscopy as
process analytical technology**

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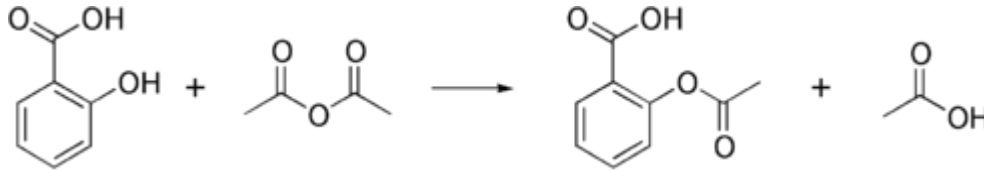
Rhonda Fenwick, *Time is Now I*
Through her art, Rhonda has explored psoriasis, a
chronic skin disorder she has lived with since the age
of six.

Outline

- Introduction to Process analytical technology (PAT)
- IR spectroscopy: endpoint determination
- Model averaging approach to reaction trends
- Discussion

API synthesis: reaction monitoring

- Reaction for the synthesis of aspirin*:



- Goal of the process chemist:
 - ✓ Optimize reaction conditions
 - ✓ Maximize yield
 - ✓ Minimize side products
 - ✓ Maintain robustness of reaction for long period of time (up to 24 h)

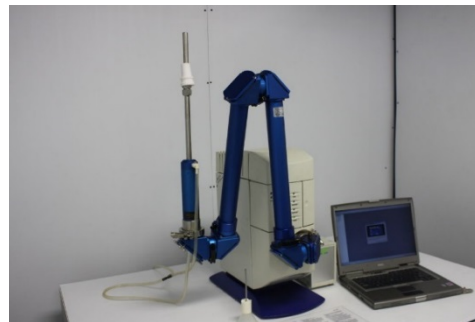
* <https://en.wikipedia.org/wiki/Aspirin>

PAT for reaction monitoring

PAT is a system to monitor and control the process, e.g. synthesis of API in the lab



'Offline' way: take a sample and measure in a separate lab



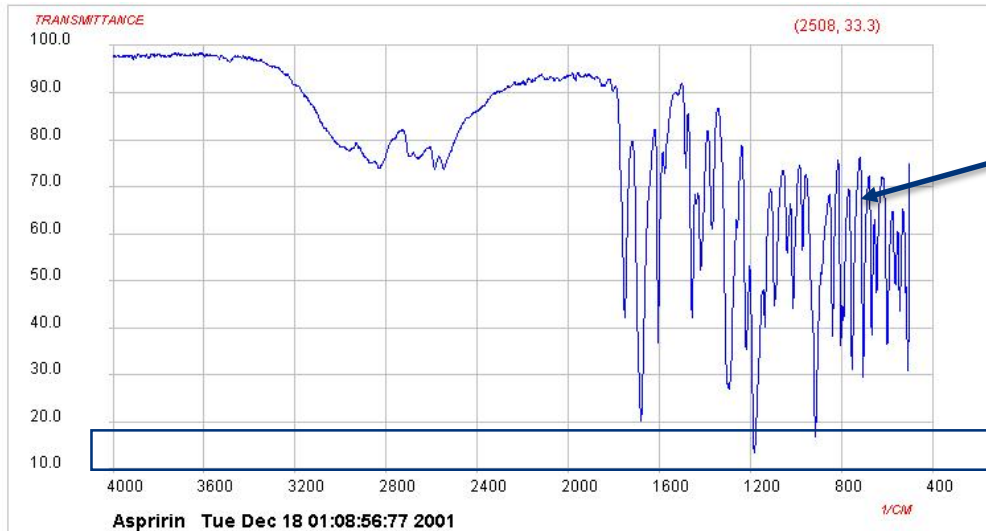
'Online' way: measure during reaction

Advantages of PAT:

- ✓Fast
- ✓Not laborious
- ✓Continuous monitoring

PAT: (mid)infrared (m-IR) spectroscopy

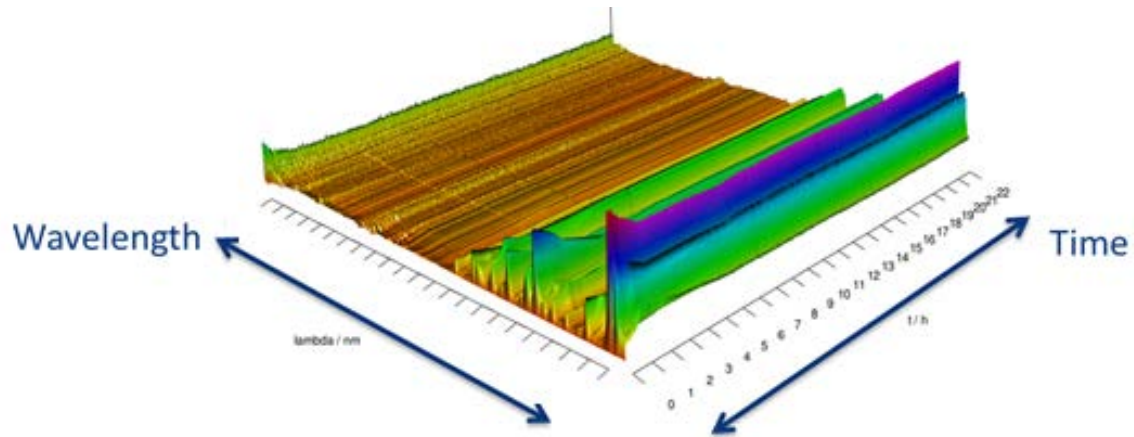
- m-IR continuously measures relative concentrations of reaction components
- For each measurement a spectrum of values is provided:



Peaks (height of the peak proportional to concentration)

Wave numbers

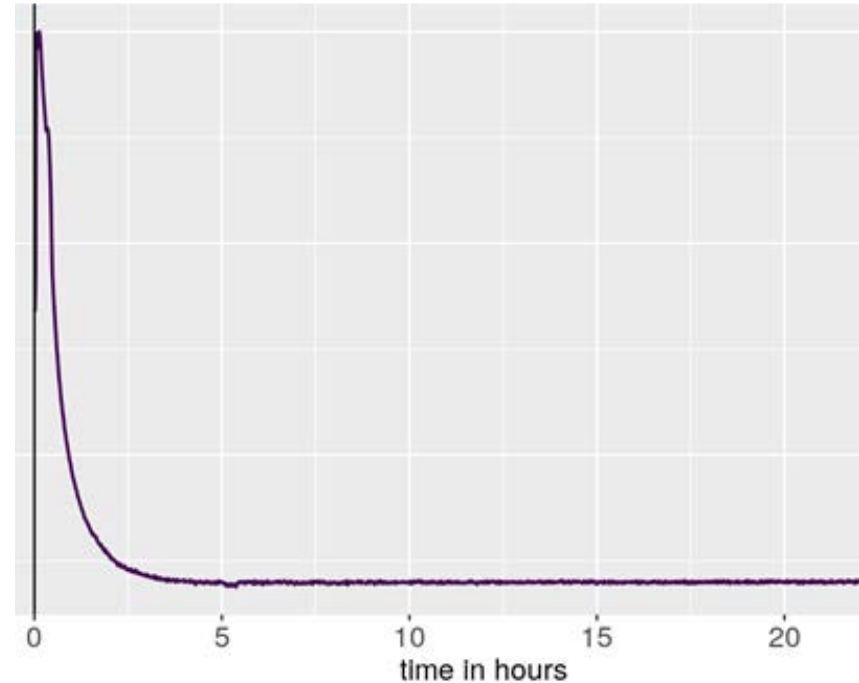
PAT data: a 3D plot



(3D image is created by spectralAnalysis R package).

Data: motivating example

- IR spectra of ~24 hours reaction (in total >1000 timepoints).
- Preprocessing:
 - ✓ baseline corrected
 - ✓ normalized
 - ✓ reaction start time determination
 - ✓ Extracted known peak of starting material (univariate):



Motivating research question: Endpoint

- **Definition of endpoint**

time when all starting material (SM) has been consumed and no more final product can be formed.

- **Data-driven definition of endpoint**

Criterion	Data Type	Challenge
SM < 1%	Offline	Online processing require extra calibration
No change in the trend of SM	Online	Threshold dependent
SM consumed > 99%	Online	Rescaling of the trend

Methodology

- An experiment-wise method:
 1. Fit parametric non-linear model.
 2. Construct (a) confidence interval on asymptote (end value) and (b) prediction interval on trend
 3. The uncertainty in model shape/choice of the model is accounted by model averaging.

Non-linear modelling

- Models for non-linear degradation kinetics:
 1. $Y_t = A + be^{-rt}$: exponential decay of the 1st order.
 2. $Y_t = A + be^{-rt^n}$: exponential decay of the n^{th} order.
 3. $Y_t = A + b_1e^{-rt} + b_2e^{-(r+s)t}$: biexponential decay (reparametrized to avoid label switching).
- Other functions can be added depending on the knowledge of kinetics.

Model averaging and interval estimation

The method of Burnham and Anderson (2003) based on AIC is applied:

1. Model averaged estimator of a model parameter

$$\hat{\theta} = \sum w_i \theta_i ,$$

where w_i are weights calculated over the model.

2. If AIC is used for weights (as in our case)

$$w_i = e^{-0.5\Delta_i} / \sum e^{-0.5\Delta_i} ,$$

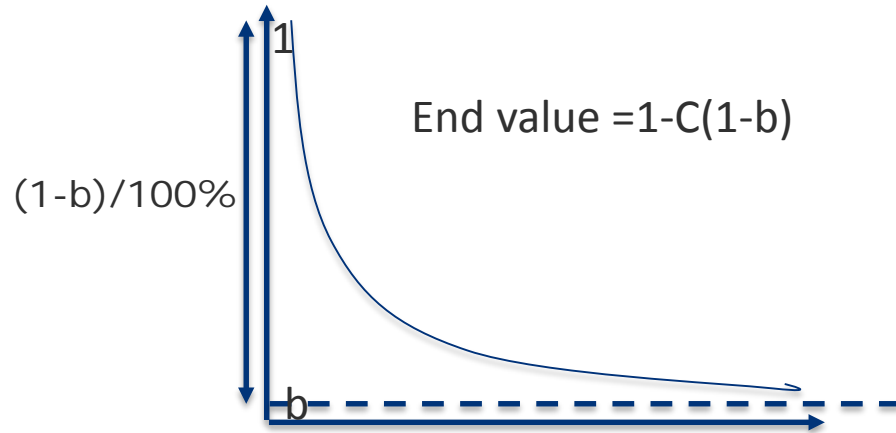
where Δ_i is a difference in weight with best model.

3. The variance of the model-averaged estimator is then

$$\widehat{Var}(\hat{\theta}) = \left[\sum w_i \sqrt{var(\hat{\theta}_i | g_i) + (\theta_i - \bar{\theta})^2} \right]^2 .$$

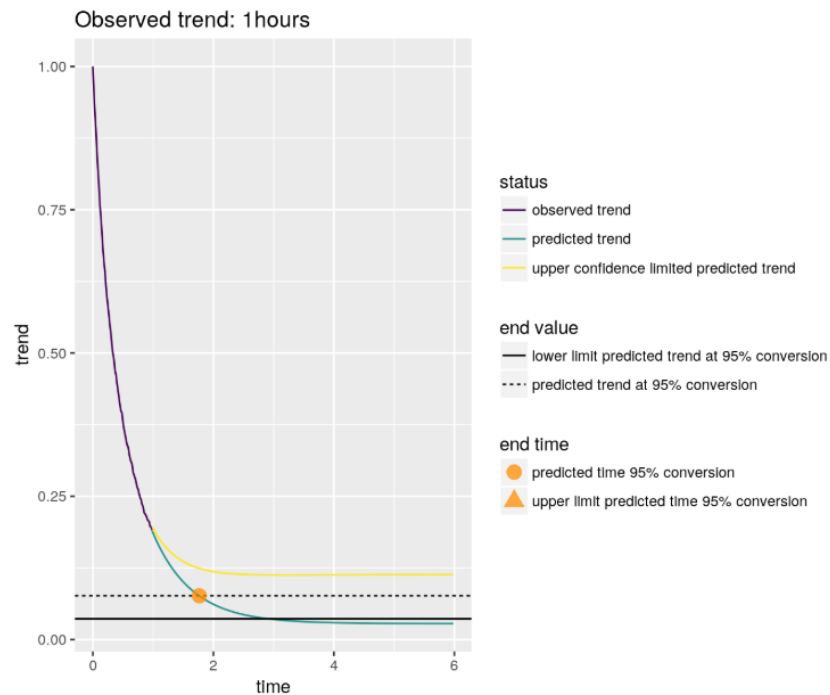
4. Based on the estimate and its variance the 95% confidence interval will be constructed using Z-method.

Endpoint calculation based on the interval estimates

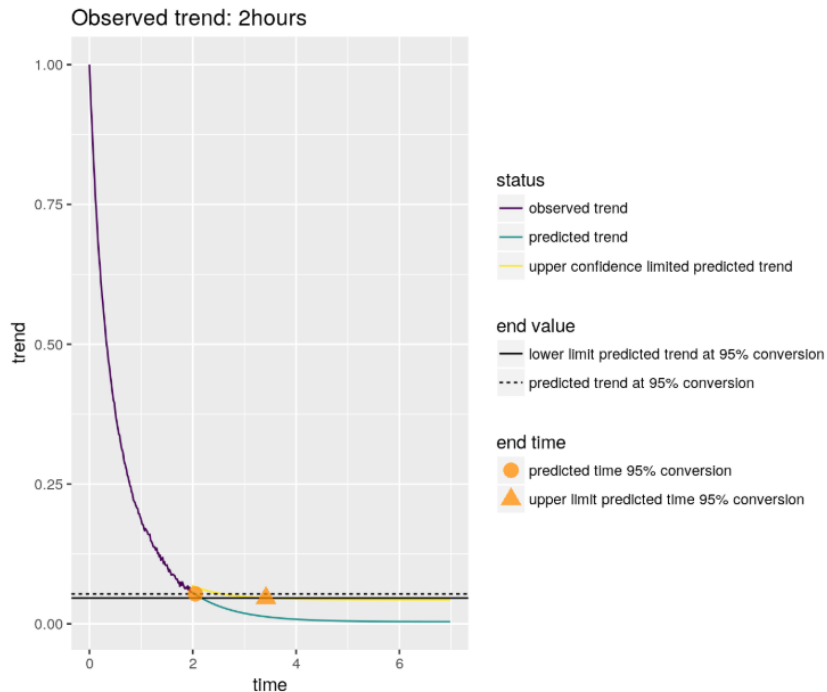


1. Obtain 95% lower confidence limit for the asymptote of the process (estimate of the end value).
2. Obtain 95% upper prediction limit for the trend using delta-method.
3. Obtain the estimate of the conversion time at desired level (e.g. $C=95\%$, 97% , $99\%...$) using direct calculation.
4. Get the predicted time and the upper 95% confidence limit of the time as follows:
 - endpoint time = time when predicted trend has reached 1% (in case observed did not reach this limit);
 - upper 95% limit of the endpoint time = the first time when the lower 95% LCL of the asymptote is reached by the 95% UPL of the trend.

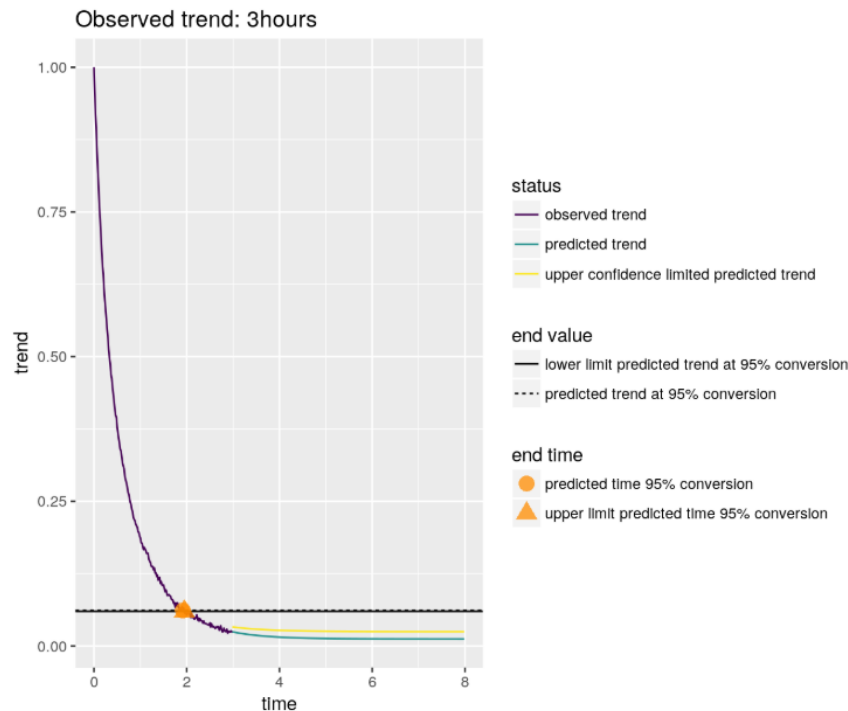
Endpoint detection: illustration



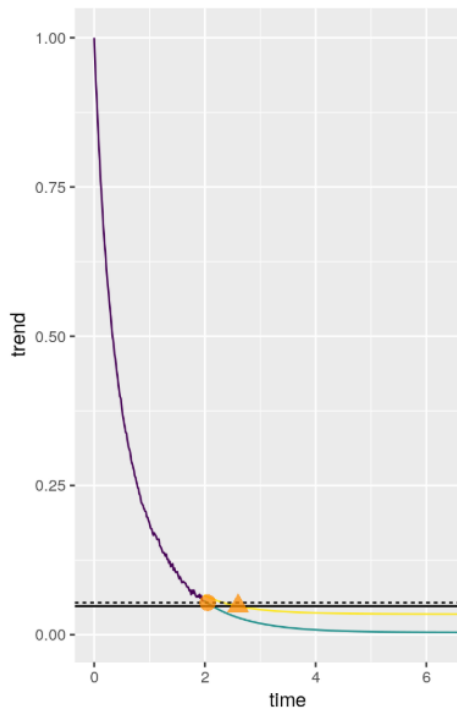
Endpoint detection: illustration



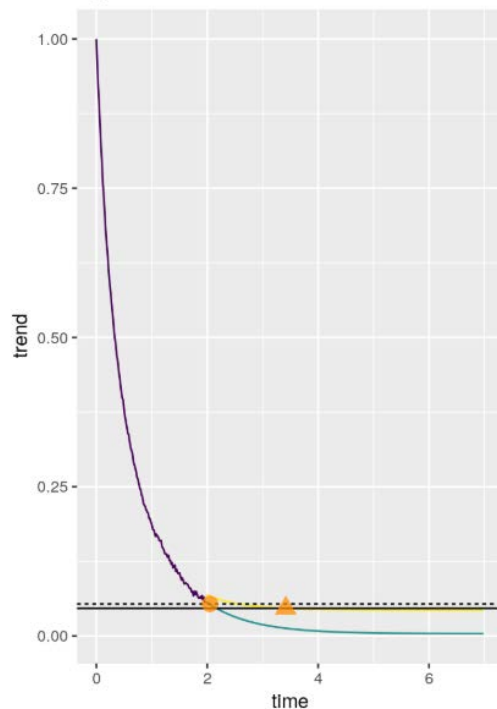
Endpoint detection: illustration



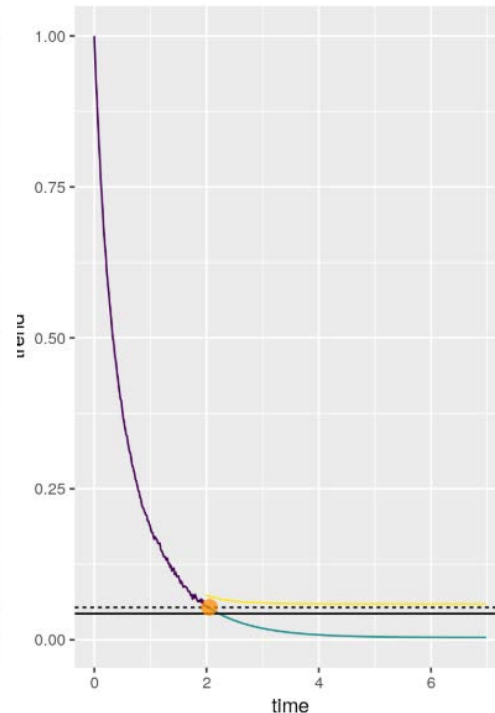
Endpoint detection wrt Confidence Level



90% confidence level

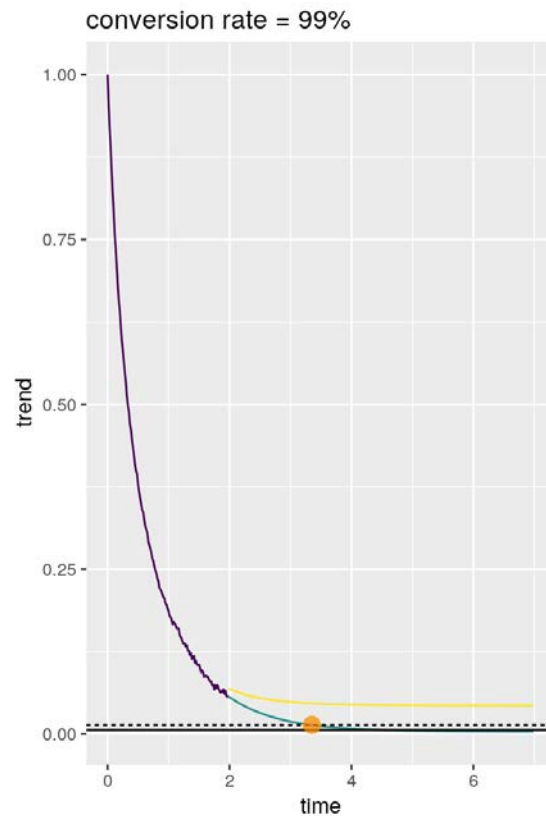
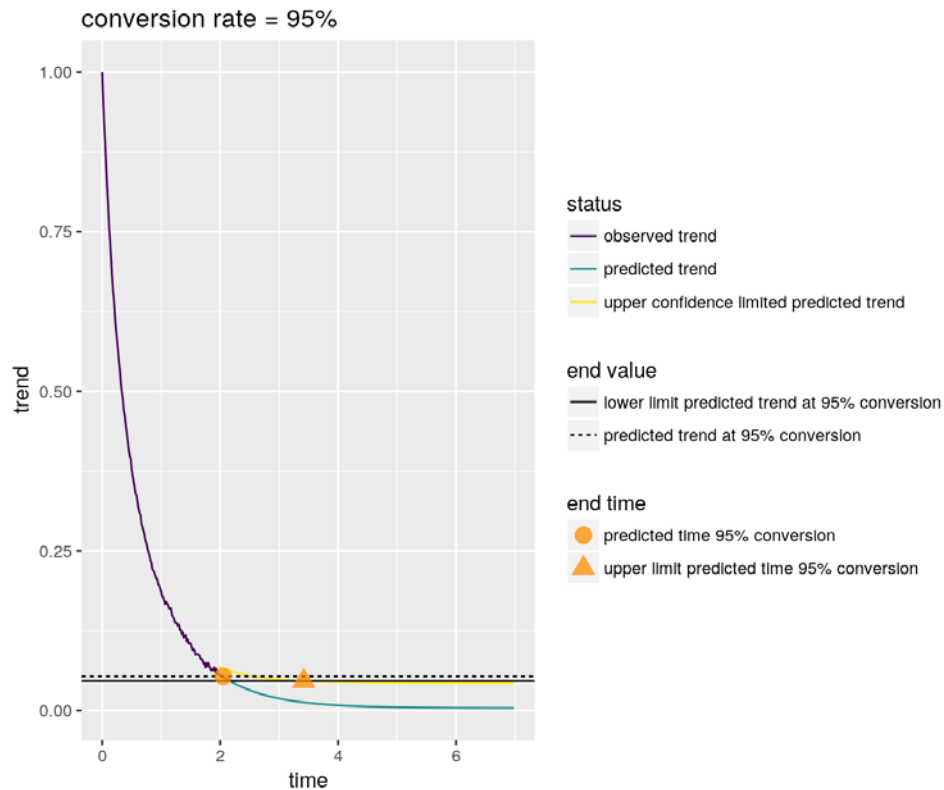


95% confidence level



99% confidence level

Endpoint detection wrt endpoint definition



Discussion: Advantages

- Real-time data processing by non-linear modelling.
- No external calibration needed.
- No extra experimental runs required.
- Flexible set of kinetic models.

Discussion: Limitations

- Reaction start point uncertainty.
- Sensitivity to choice of conversion percentage.
- Noise in online PAT measurements.

Assumptions and further research

- Conversion is reached at asymptote.
- No drift in measurements (cfr. heat-generating process).
- Normal distribution of the residuals.
- Separate construction of the intervals.
- Bayesian paradigm (simultaneous estimation) may be unfeasible for online application.
- Parametric bootstrap.

Conclusions

- IR spectroscopy allows for online monitoring of chemical processes.
- The generated IR data can be used for real time endpoint detection in development phase.
- Non-linear modelling together with model averaging are tools for real-time prediction which are experiment-specific.
- Some further research and extensions are needed to make this methodology applicable for a variety of processes.

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References

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- (2) Guidance for Industry PAT — A Framework for Innovative Pharmaceutical Development, Manufacturing, and Quality Assurance (2004). FDA guidance: Pharmaceutical CGMPs.
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- (4) R package spectralAnalysis: <https://cran.r-project.org/web/packages/spectralAnalysis/index.html>



Thank you!

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