



**Mixed models using the SAS®
PROC MIXED procedure:**

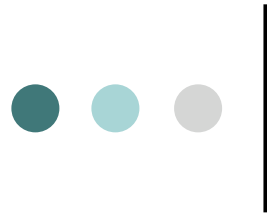
**A simulation based approach to
assess sample size and resolve a
daily biostatistician's dilemma for
preclinical trials...**

Louise Baschet – Catherine Hessler



SFDS Working Group

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 - A. De Montfort, C. Hessler (*sanofi pasteur*)
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 - C. Phalyvong (*SOLADIS*)



Our context: preclinical research area

- Seen by the biologist
 - Comparison between treatments
 - Limited number of subjects
 - Repeated measures over time
- Seen by the statistician
 - Many experiments related to longitudinal data
 - Small sample size
 - Potentially missing data



Our context: preclinical research area

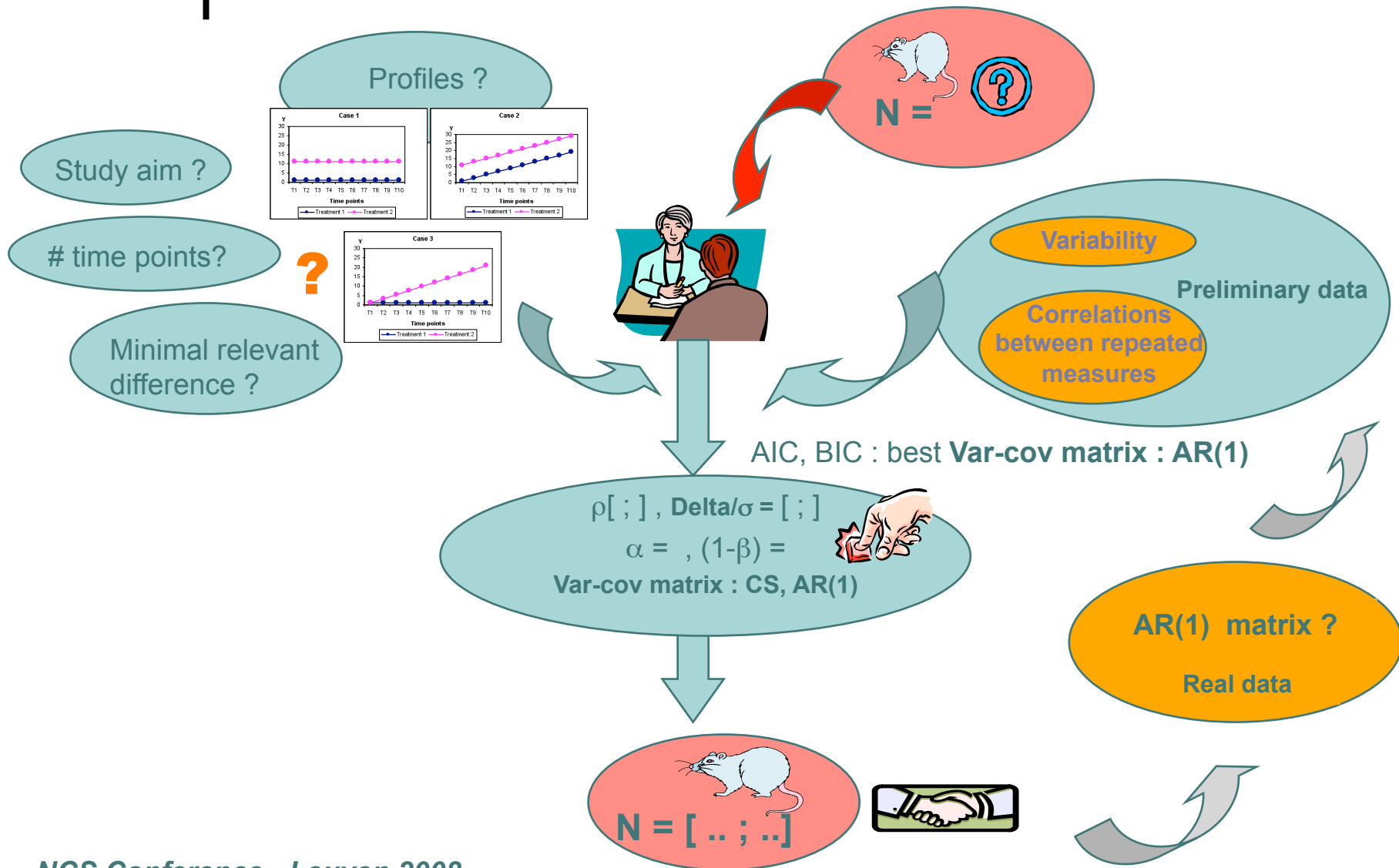
- Seen by the biologist
 - Comparison between treatments
 - Limited number of subjects
 - Repeated measures over time
- Seen by the statistician
 - Many experiments related to longitudinal data
 - Small sample size
 - Potentially missing data
- ↳ Proc mixed is commonly used
 - More suitable than GLM for repeated measures
 - Management of missing data
 - Better modeling of the correlations between observations
- But
 - Multiple options not well understood to date
 - Choice of the var/cov structure sometimes tricky



Objectives

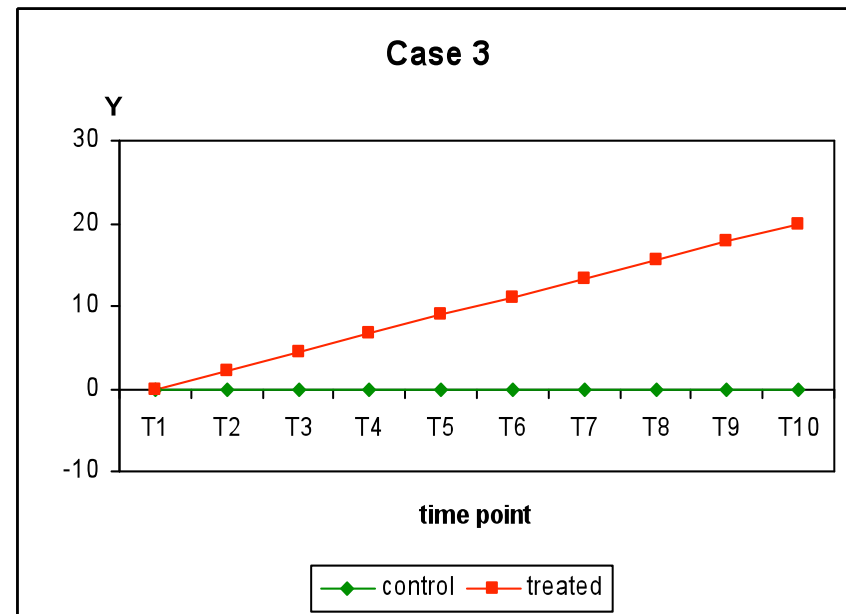
- Evaluate the impact of various options in the proc mixed
 - on alpha
 - on power
- Provide sample size evaluation by a simulation program

Strategy for sample size evaluation



Studied designs

- Classical and simple experimental design
 - 2 groups (control and treated)
 - Repeated measures over time
- Focus on 4 common response profiles
 - With or without interaction and effect
 - 3 and 10 time points



	case 0	case 1	case 2	case 3
interaction	0	0	0	X
treatment	0	X	X	X
time	0	0	X	X

● ● ● | Simulation approach for each case

1000 to 2000 times

Simulation

- 2 samples with CS or AR(1) structure
- Corr = 0.2 or 0.8
- 3 or 10 time points
- n = 4 to 14 by 2
- Delta = 10, Sigma = 10

X

Analysis

- ML or REML **method**
 - CS or AR(1) Var-covar **matrix**
- model

=

Result

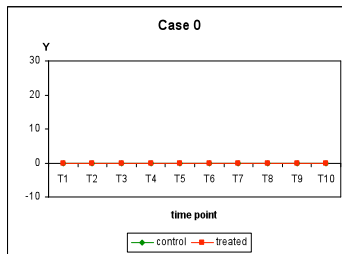
- Count of significant p-values for :
- Group effect according to interaction
 - Interaction
 - Time effect



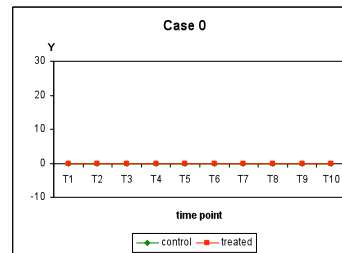
● ● ● | α -level control

- Simulations under H0
 - α threshold: 10%

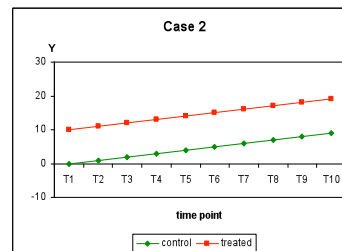
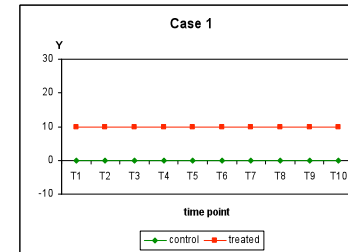
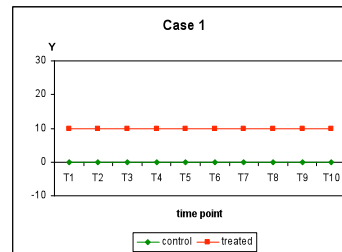
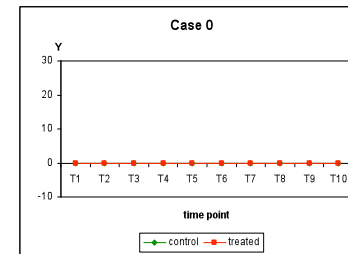
No group effect



No interaction effect



No time effect



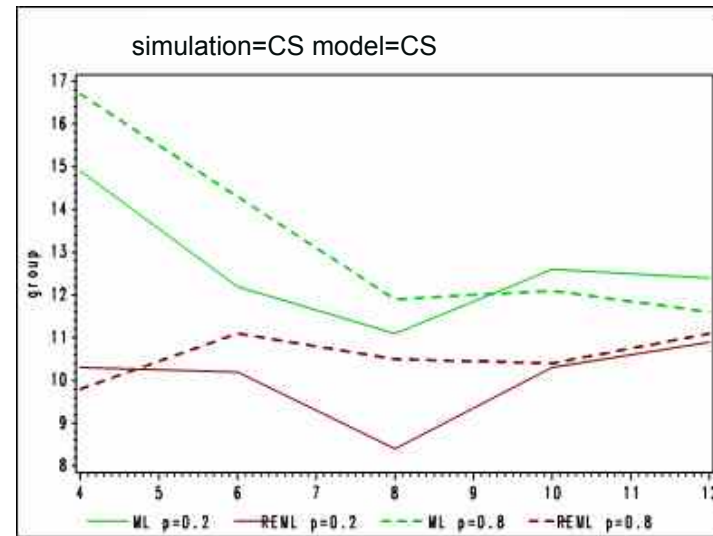
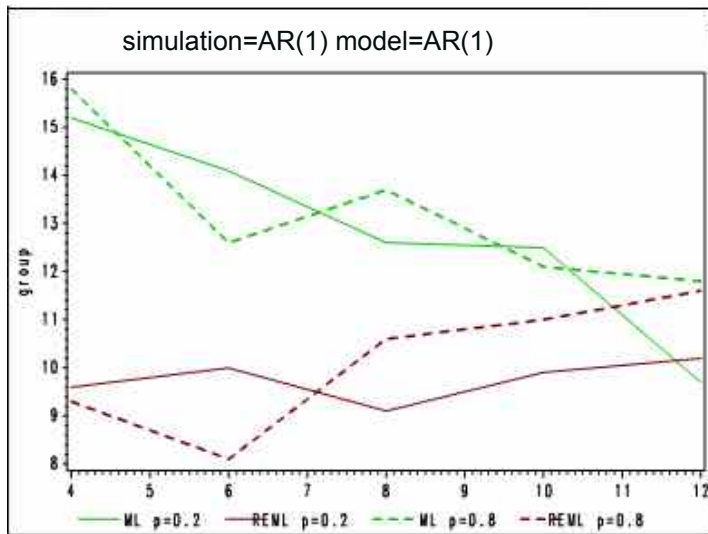


α -level control

- Results (1): method

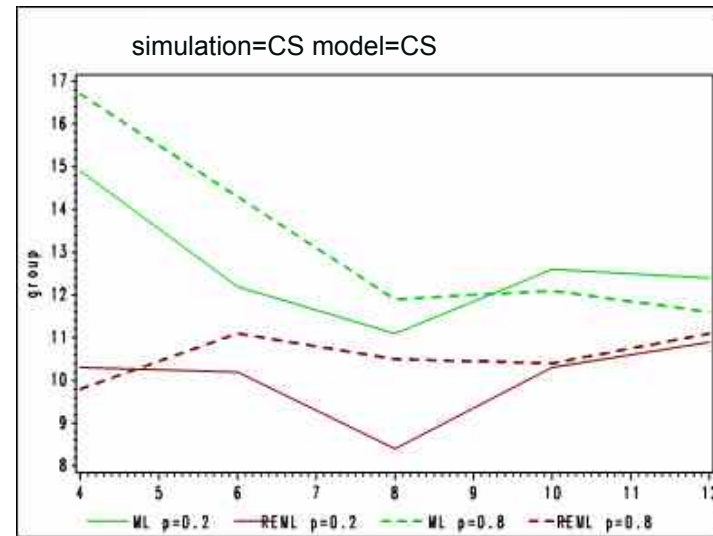
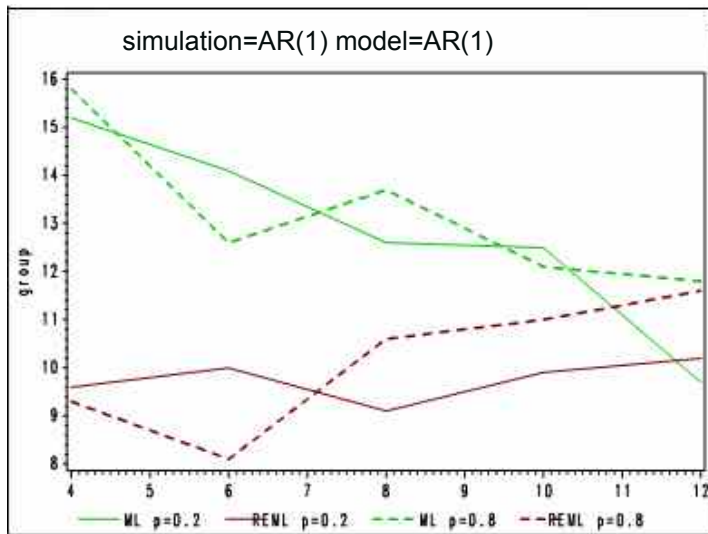
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- Results (1): method
 - With ML, α is uncontrolled for some very low sample size!



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↪ REML is kept afterwards



α -level control

- Results (2): variance-covariance matrix



α -level control

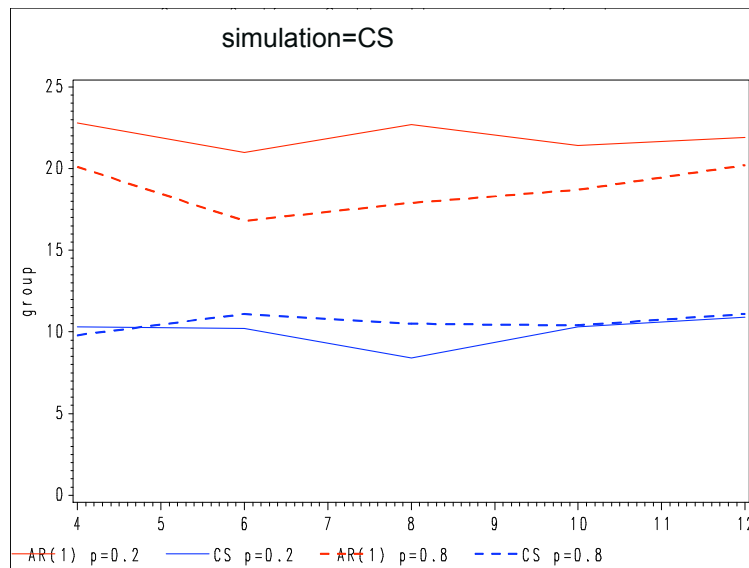
- Results (2): variance-covariance matrix
 - For group effect:

● ● ● | α -level control

- Results (2): variance-covariance matrix

- For group effect:

- If analyzed with AR(1), α risk is increased for a CS structure

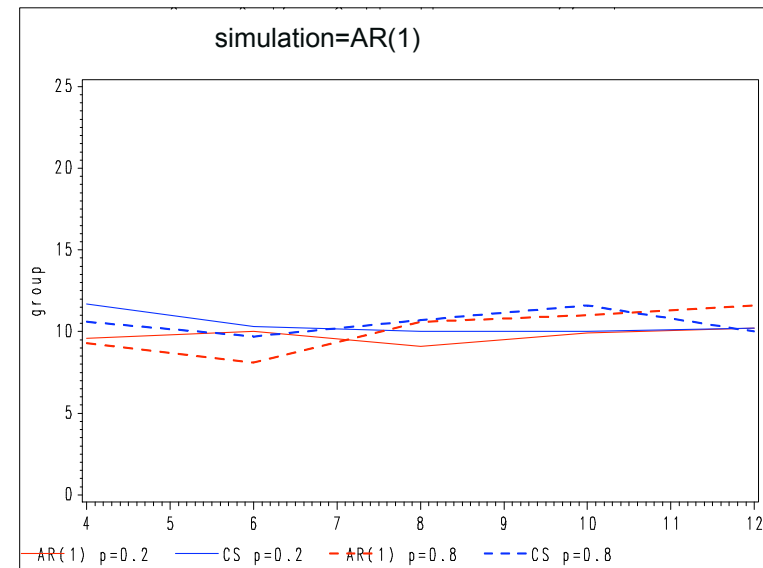
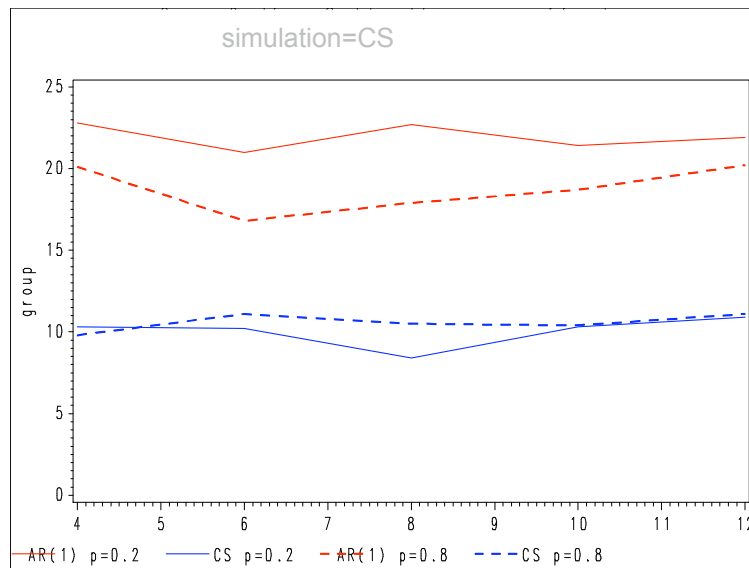


● ● ● | α -level control

○ Results (2): variance-covariance matrix

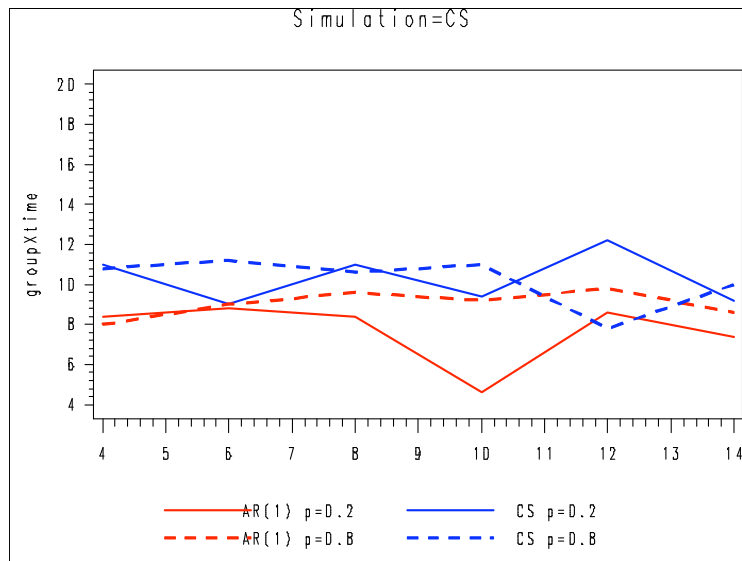
● For group effect:

- If analyzed with AR(1), α risk is increased for a CS structure
- No impact of the matrices for a **AR(1)** structure



● ● ● | α -level control

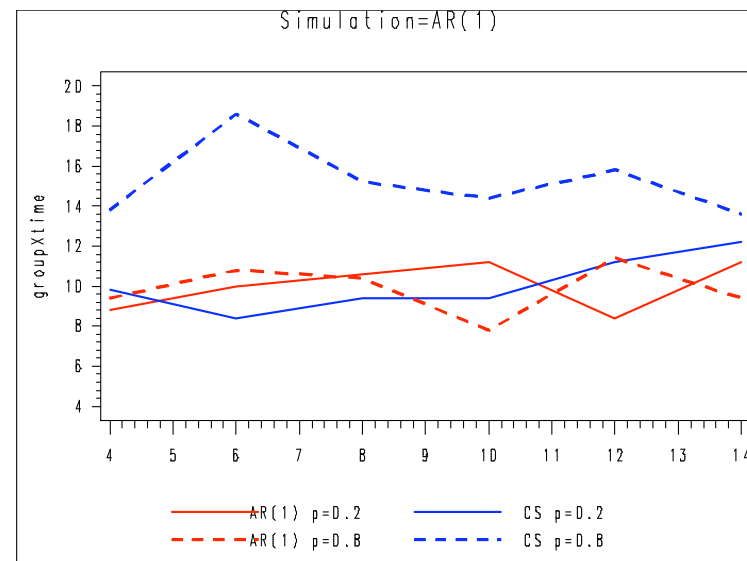
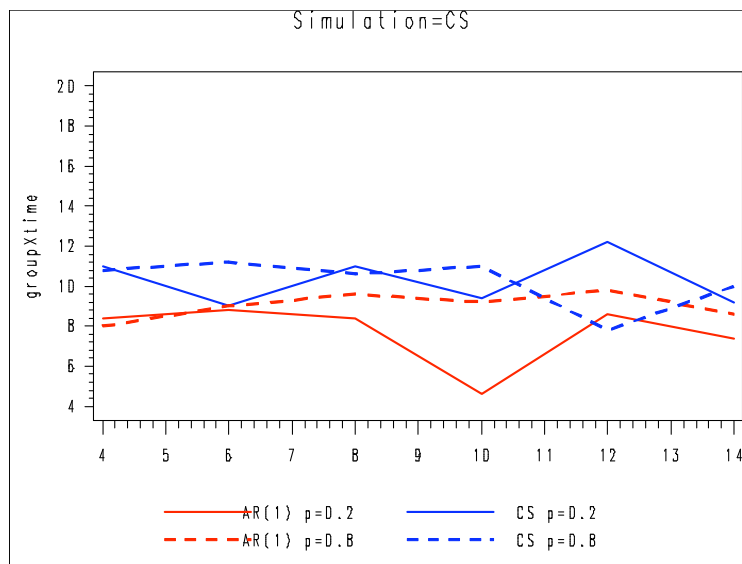
- Results (2): variance-covariance matrix
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● ● ● | α -level control

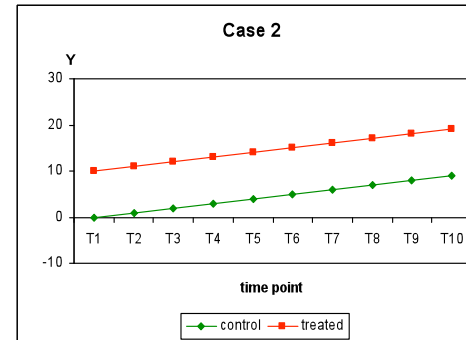
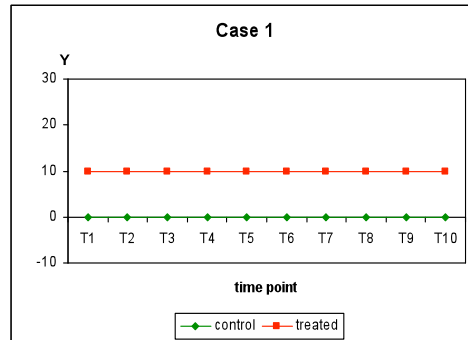
○ Results (2): variance-covariance matrix

- For interaction effect:
 - No impact of the matrices for a CS structure
 - If analyzed with CS α risk is increased for a AR(1) structure when ρ is high
- Conclusions are the same for time effect



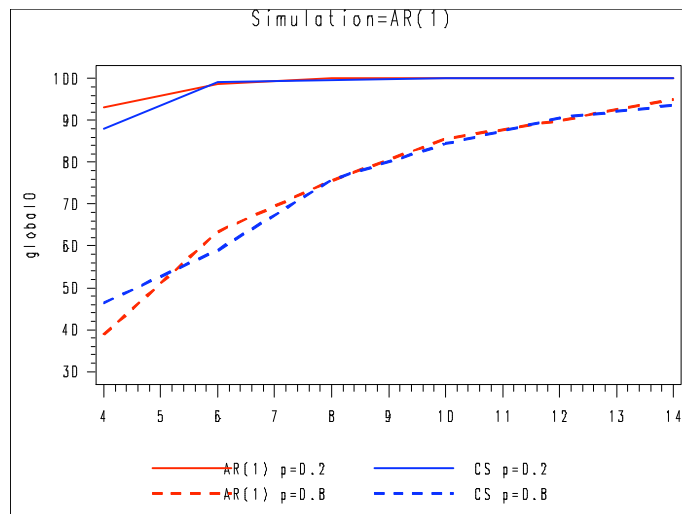
Impact of the variance-covariance matrix on power for the group effect

- Without interaction (cases 1 and 2)



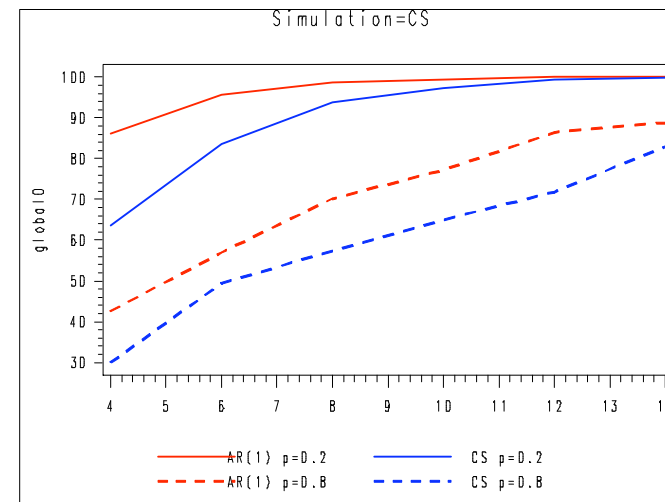
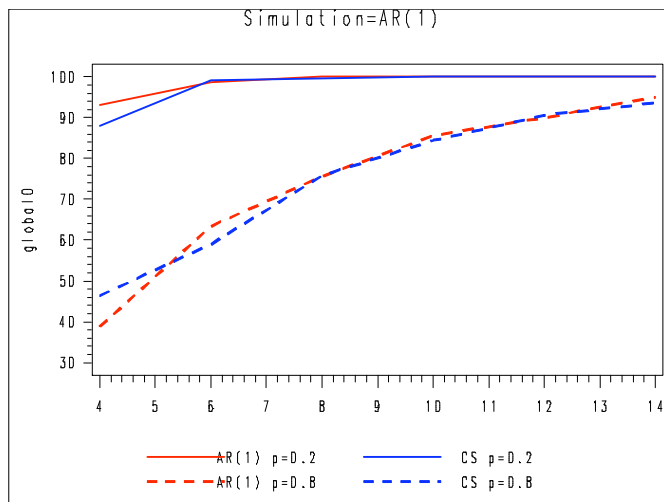
Impact of the variance-covariance matrix on power for the group effect

- Without interaction (cases 1 and 2)
 - For a data structure **AR(1)**
 - no impact of the matrices
 - power is higher as ρ is lower



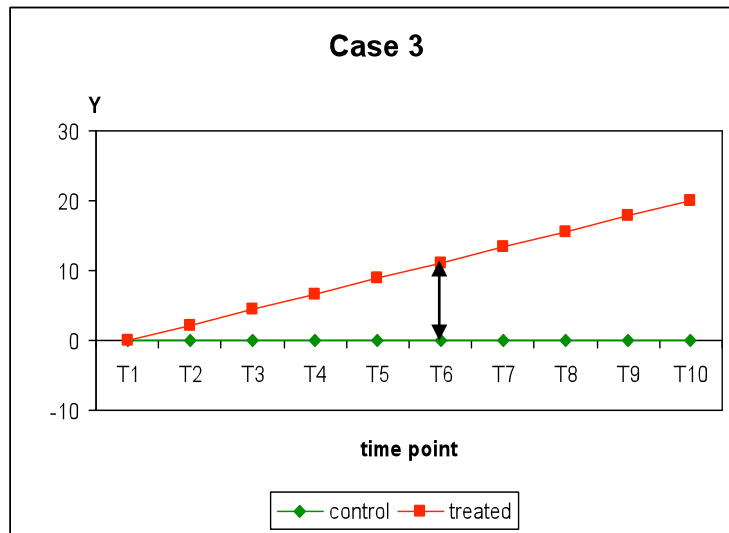
Impact of the variance-covariance matrix on power for the group effect

- Without interaction (cases 1 and 2)
 - For a data structure AR(1)
 - no impact of the matrices
 - power is higher as ρ is lower
 - For a data structure CS
 - AR(1) analysis gives a higher power
 - power is higher as ρ is lower



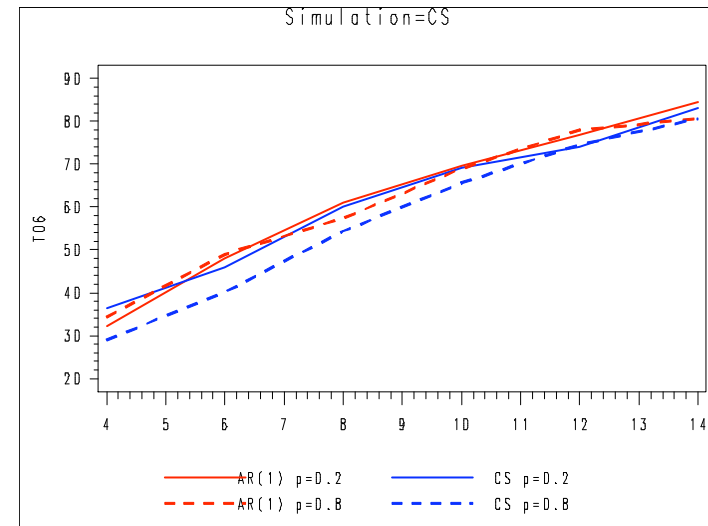
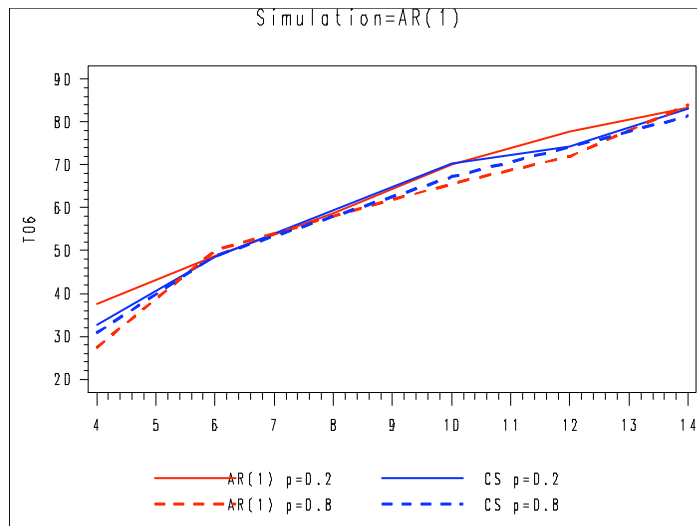
Impact of the variance-covariance matrix on power for the group effect


- With interaction (case 3)
 - At the middle time-point (T6)



Impact of the variance-covariance matrix on power for the group effect


- With interaction (case 3)
 - At the middle time-point (T6)
 - no impact of ρ and matrices





Impact of the variance-covariance matrix on power for the interaction and time effect

- Interaction effect (case 3)
 - Whatever the data structure is
 - power is higher with **CS**
 - especially when ρ is high



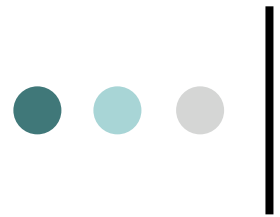
Impact of the variance-covariance matrix on power for the interaction and time effect

- Interaction effect (case 3)
 - Whatever the data structure is
 - power is higher with **CS**
 - especially when ρ is high
- Time effect without any interaction (case 2)
 - Whatever the data structure is
 - power is higher with **CS**
 - especially when ρ is high



Conclusion

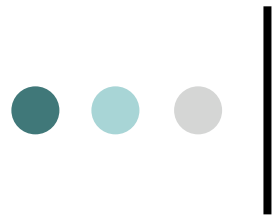
- REML has to be chosen to control the α -risk



Conclusion

- REML has to be chosen to control the α -risk

	To control α	To maximize $(1-\beta)$
Group effect	CS	AR(1)
Interaction or time effect	AR(1)	CS



Conclusion

- REML has to be chosen to control the α -risk
- It is recommended to choose the matrix according to the primary objective

	To control α	To maximize $(1-\beta)$	To estimate n (<i>worst case</i>)
Group effect	CS	AR(1)	CS
Interaction or time effect	AR(1)	CS	AR(1)



Perspectives

- Missing and/or unbalanced data
- Heterogeneous variances
- More than 2 groups and α adjustment
- Time as a continuous variable
- Other types of variance matrix



References

- Linear Mixed Models for Longitudinal Data, Verbeke G., Molenberghs G., Springer Series in Statistics, 2000
- Applied Mixed Models in Medicine, Brown H., Prescott R., Statistics in practice, 1999
- Tutorial in Biostatistics: Modelling covariance structure in the analysis of repeated measures data, Littell R. C. and al., Statistics in Medicine, 2000
- SAS institute, Inc. (1999) SAS/STAT user's Guide, V8. Cary, NC: SAS Institute



Model

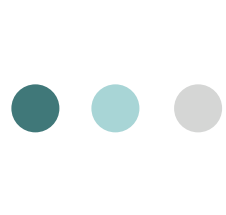
- Analysed using proc mixed with repeated statement

$$Y_{ijk} = \mu + \text{group}_i + \text{time}_j + \text{group} \times \text{time}_{ij} + \varepsilon_{ijk}$$

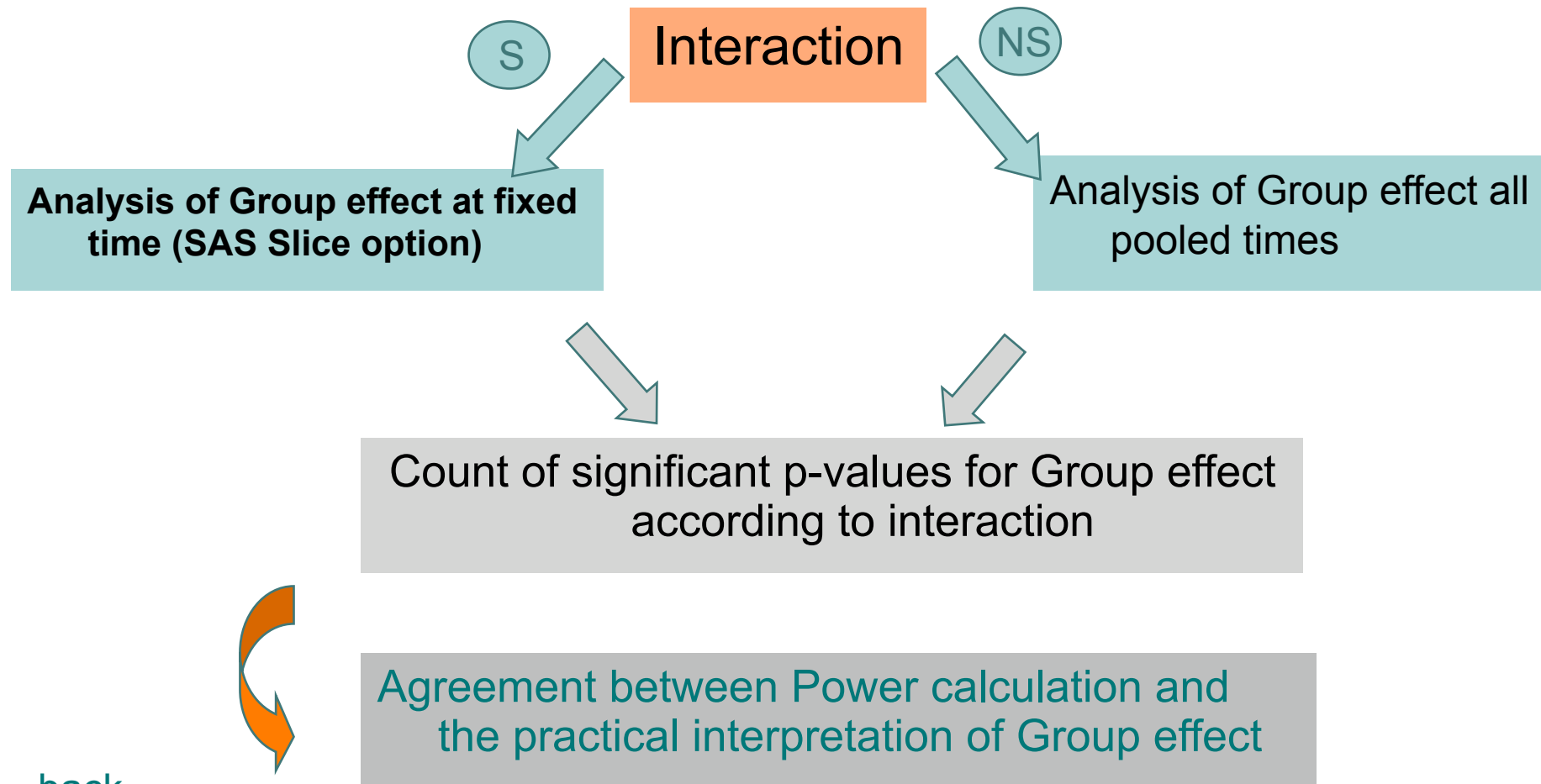
$$\varepsilon \sim \text{iid}(0, R)$$

```
proc mixed method=&method. ;  
  class group time animal ;  
  model Y = group time group*time / ddfm=satterth;  
  repeated time / subject=animal(group) type=&typvarmixed.;
```

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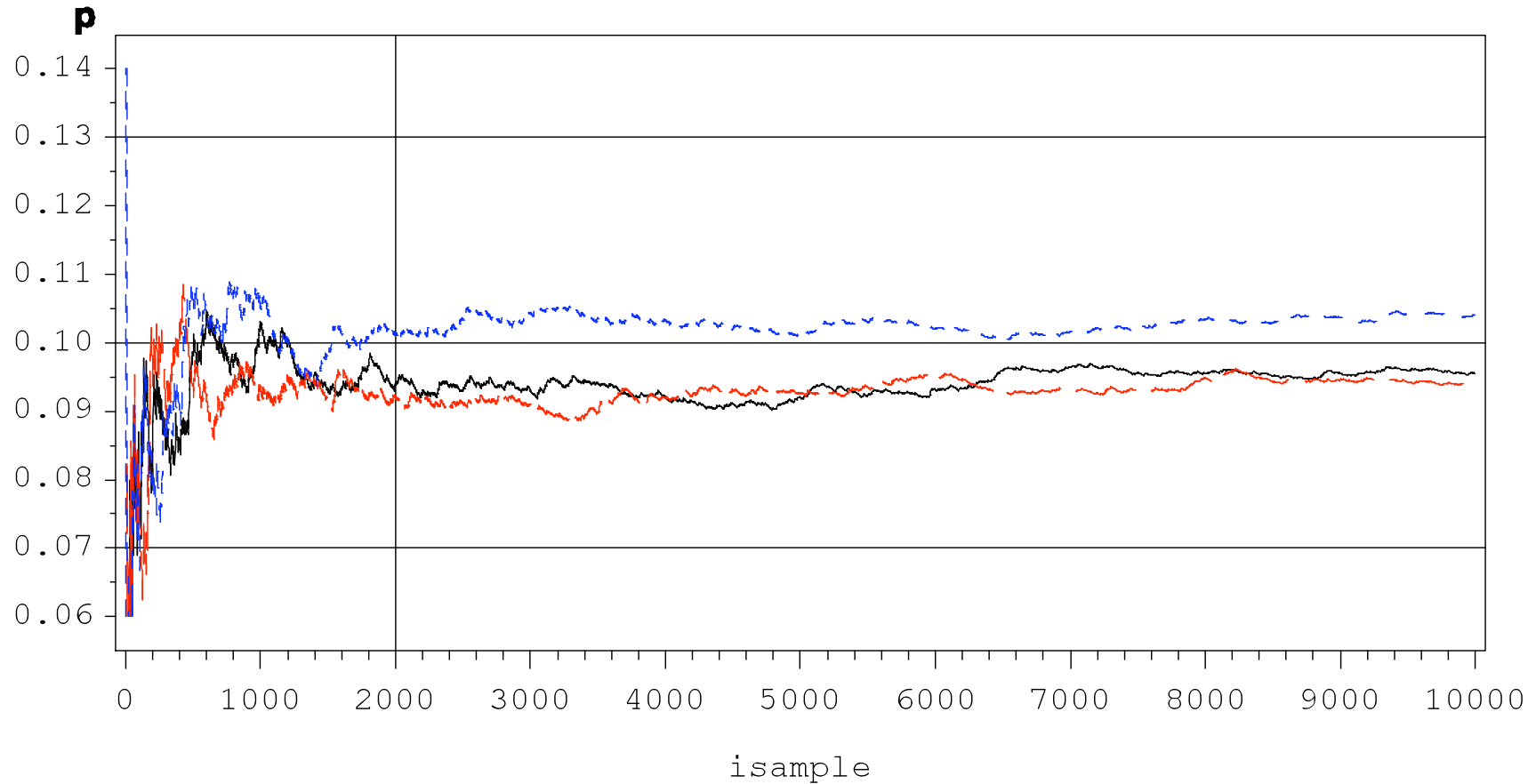
Simulation approach for each case



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3 times : rejection frequency of time effect



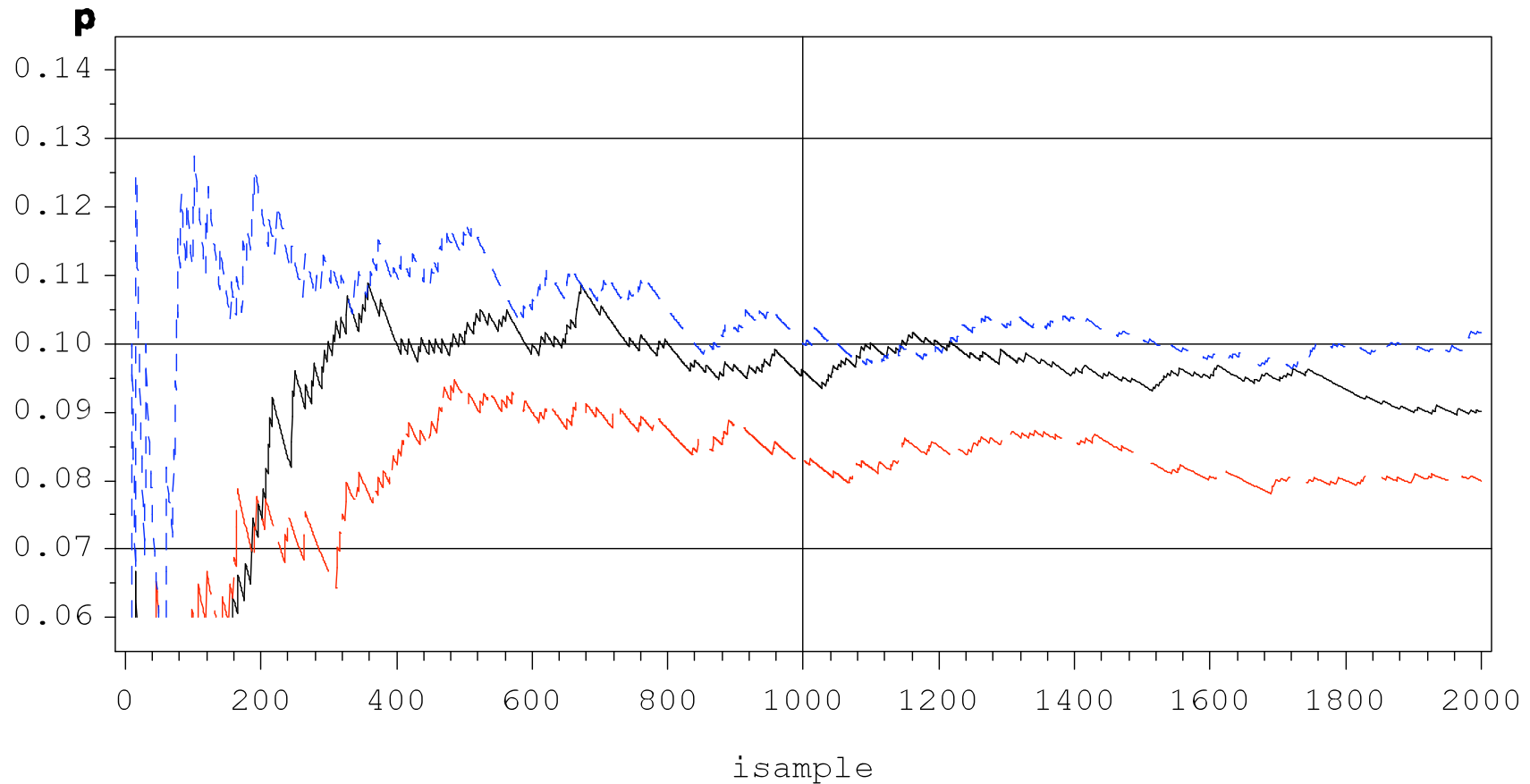
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model — AR(1) — AR1RE - - CS

[10 times →](#)



10 times : rejection frequency of time effect



[← 3 times](#)

model

— AR(1)

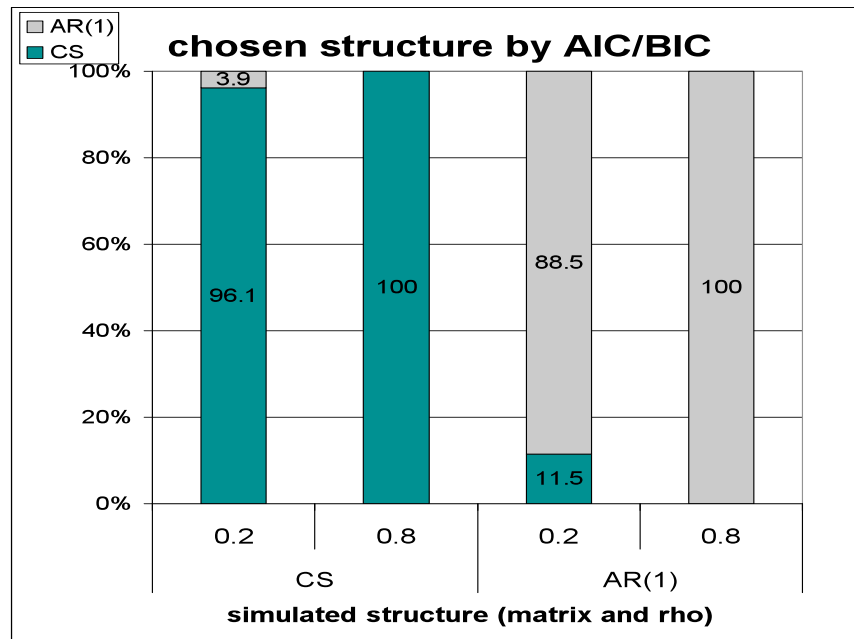
— AR1RE

- - - CS

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Use of AIC / BIC to select the suitable matrix



- Simulations are validated for these two simple structures
- **But it is possible to make mistakes is case of low correlation !**

Impact of ML and REML on α level (10 times)

1000 simulations

n = 5

			model_simul					
			AR(1)			CS		
			Effect			Effect		
			group	group*time	time	group	group*time	time
model	method	ddfm						
AR(1)	ML	Déf(BW)	11.30%	22.80%	22.10%	24.40%	18.50%	18.30%
AR(1)	ML	KR	14.20%	20.10%	19.50%	27.90%	16.30%	16.60%
AR(1)	ML	Satterth	13.20%	23.20%	22.30%	26.70%	18.50%	18.30%
CS	ML	Déf(BW)	13.30%	25.10%	23.60%	12.90%	22.70%	22.30%
CS	ML	KR	13.90%	26.00%	24.20%	14.10%	23.40%	22.90%
CS	ML	Satterth	13.90%	26.00%	24.20%	14.10%	23.40%	22.90%

			AR(1)			CS		
			Effect			Effect		
			group	group*time	time	group	group*time	time
			model	method	ddfm			
AR(1)	REML	Déf(BW)	8,10%	11,00%	10,10%	20,30%	8,70%	9,00%
AR(1)	REML	KR	10,00%	8,70%	7,90%	22,20%	6,80%	7,10%
AR(1)	REML	Satterth	8,90%	10,30%	9,50%	21,60%	8,40%	8,70%
CS	REML	Déf(BW)	9,80%	16,10%	14,90%	9,50%	9,90%	10,00%
CS	REML	KR	9,80%	16,10%	14,90%	9,50%	9,90%	10,00%
CS	REML	Satterth	9,80%	16,10%	14,90%	9,50%	9,90%	10,00%