



Non-Clinical Statistics  
Conference

2008

## Some principles of modeling and simulation in preclinical research and drug development

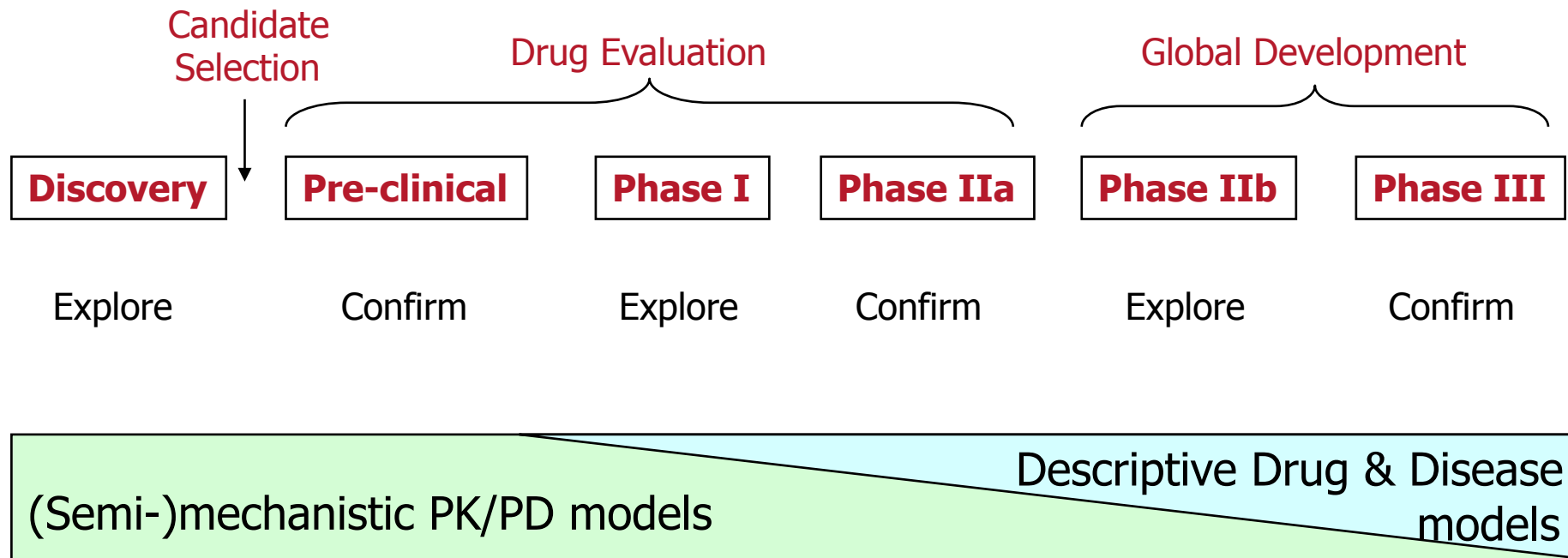
Philippe Jacqmin

*Exprimo*

# Modelling and simulations throughout drug development:

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Objectives of M&S should focus on the next phase(s) of development to support decisions that need to be made



## Mechanistic *versus* descriptive (empirical) models:

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### Mechanistic

- Early stages of development
- Good understanding of system
- Interpretable parameters
- Interpolation and extrapolation
- May require less data

### Descriptive

- Late stages of development
- Fair understanding of system (grey box)
- Less meaningful parameters
- Interpolation
- Usually requires a lot of data

# M&S throughout Discovery and Pre-clinical:

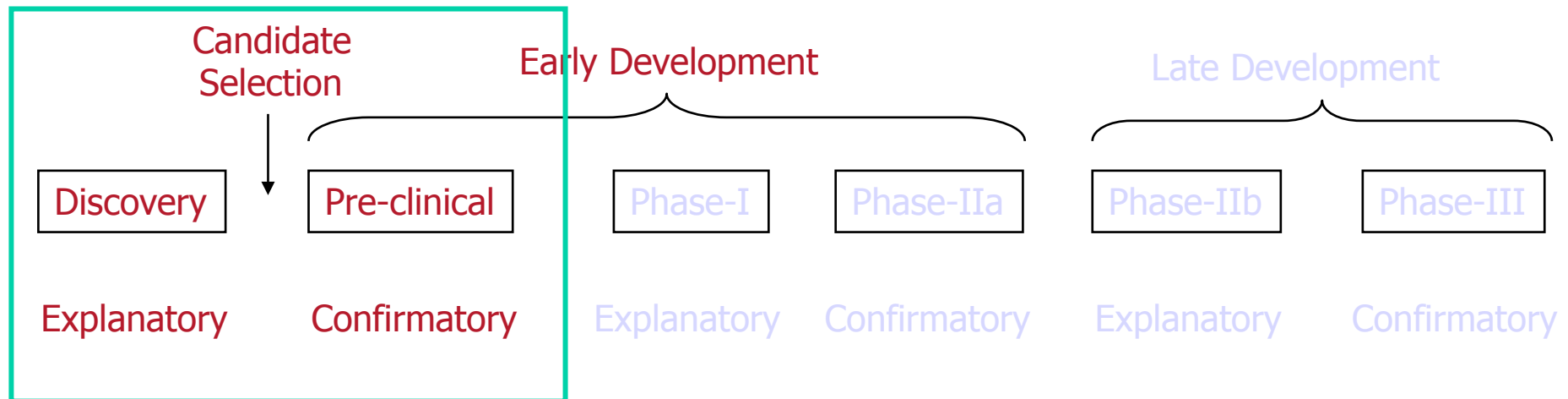
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## Current phase

- Feasibility assessment mechanism of action
- Define metrics candidate selection
- Assess safety margin
- Combined meta-analysis and objective review of all discovery and pre-clinical data

## Next phase

- Evaluation and selection appropriate biomarker(s)
- Optimize designs of early ph-I studies with biomarkers



# Why do we model in drug development?

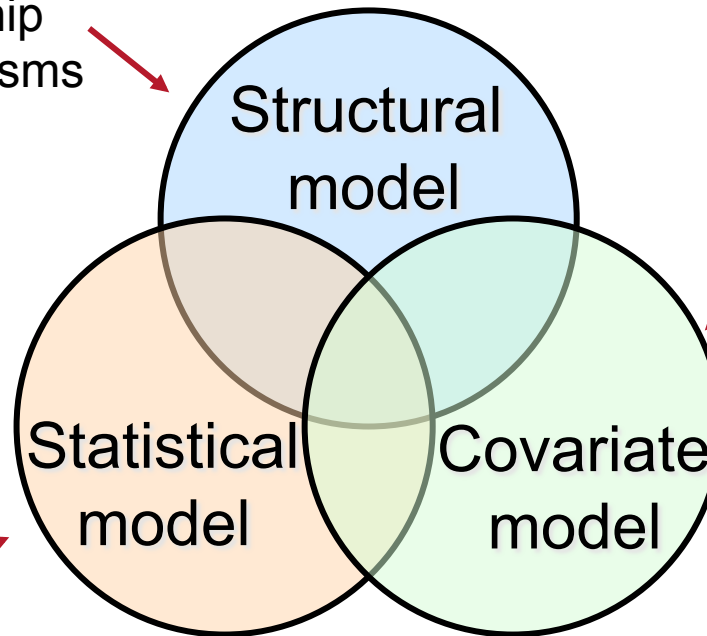
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1. The systems are complex
  - Nonlinearity and/or time dependency
  - Complex data (multiple sources, noisy, errors...)
2. To integrate information
  - Across time, dose-levels, drugs and systems
3. To predict and extrapolate
  - We are not only interested in the specific observation
  - We are often not primarily interested in the setting studied
4. To optimize further studies
5. The model can be used as a “knowledge repository”
  - Describe what is currently known about mechanism of action and system
6. The model might help to fill in the “gaps” in data
7. The model can help us identify and quantify uncertainty

# Components of drug models

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e.g. Dose-Conc. relationship  
Conc.-Effect relationship  
Physiological mechanisms  
Maturation processes

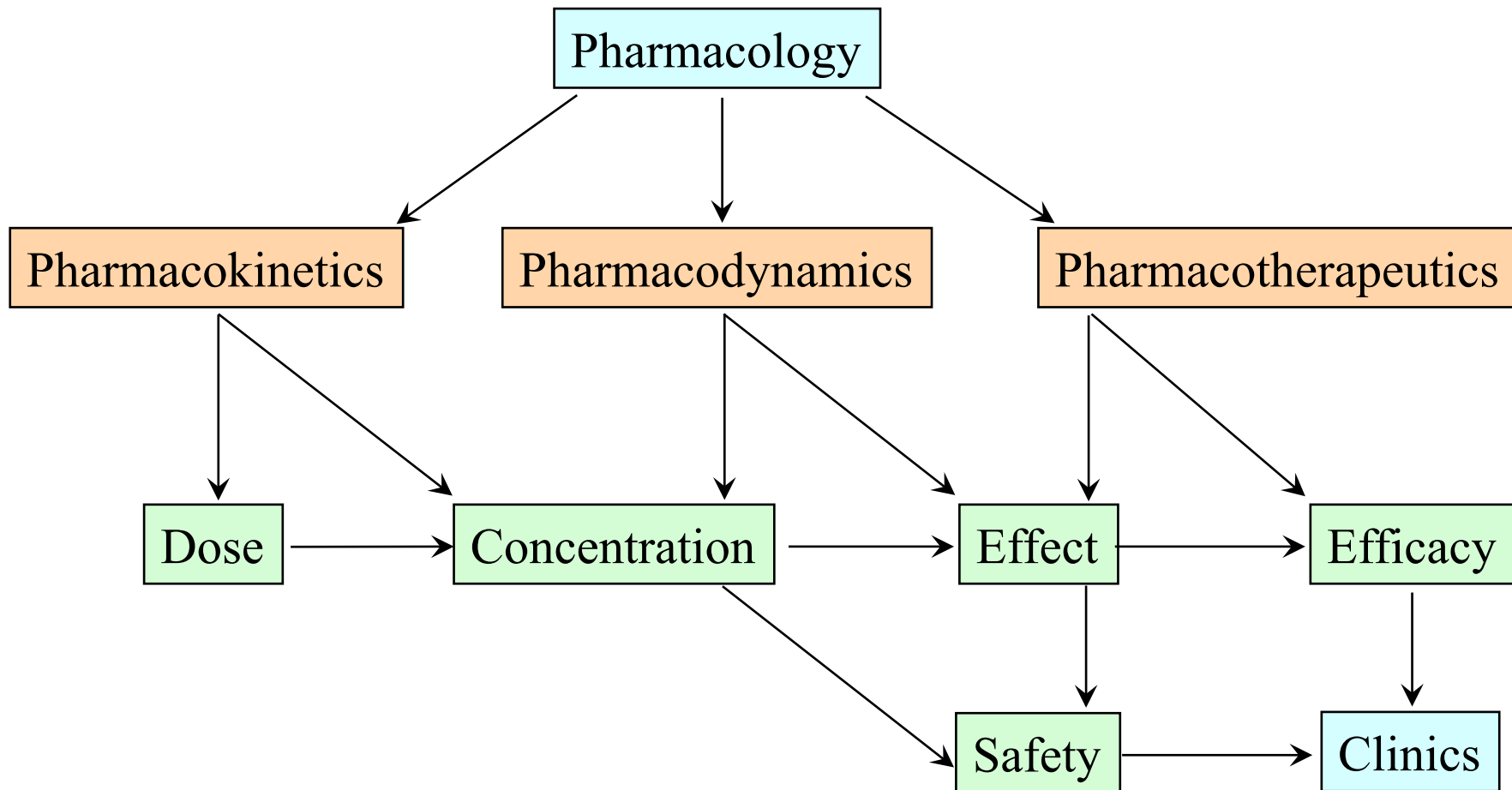


Relationships  
between parameters  
and compound/  
system  
characteristics

Inter-individual, inter-occasion  
and residual variabilities  
Uncertainty and correlation

# Pharmacokinetic-Pharmacodynamic modelling

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# Pharmacokinetic models

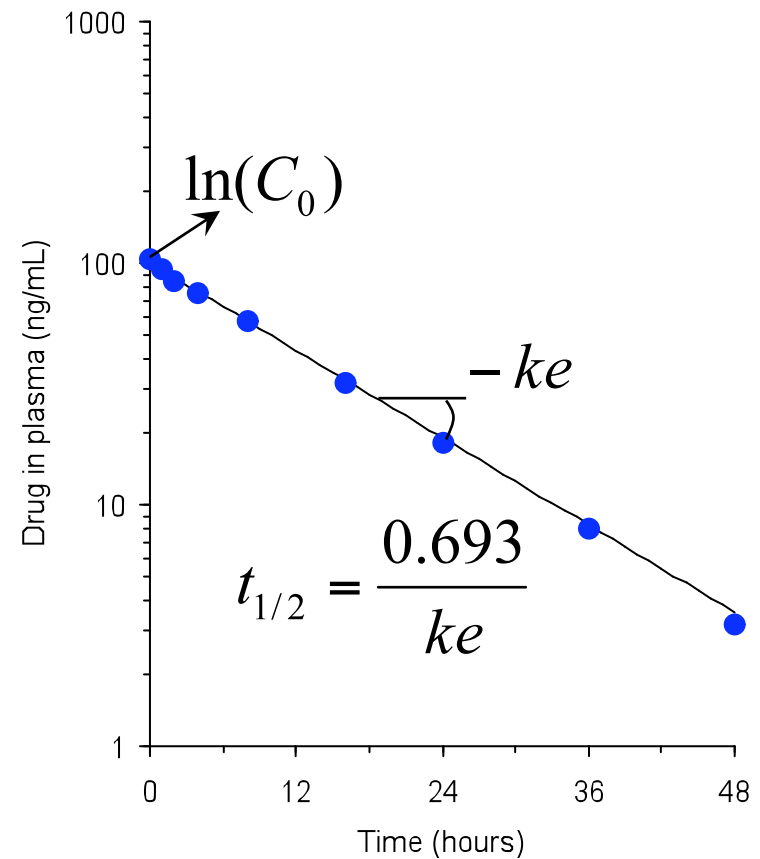
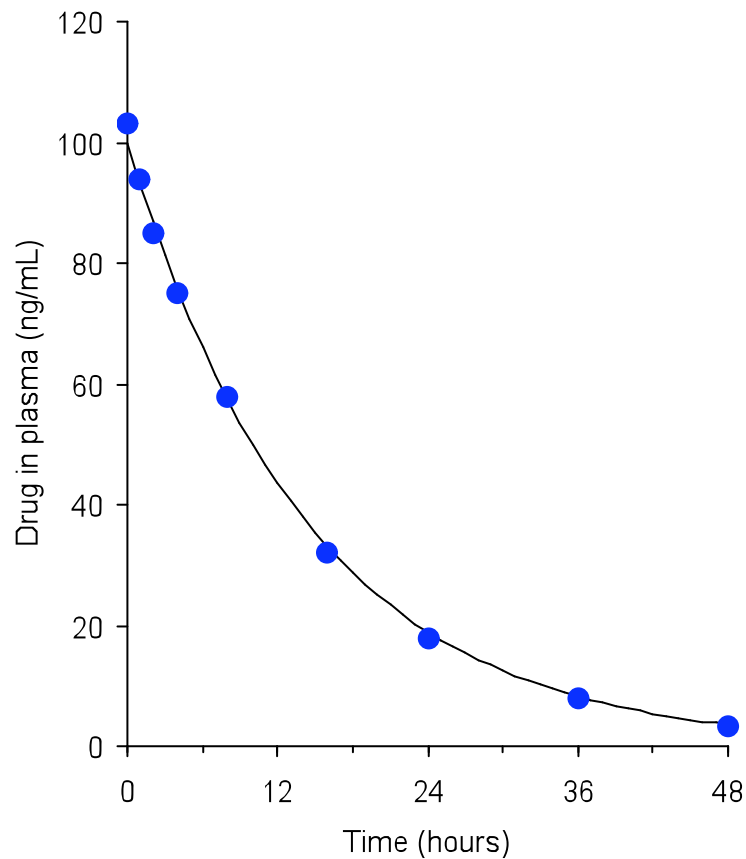




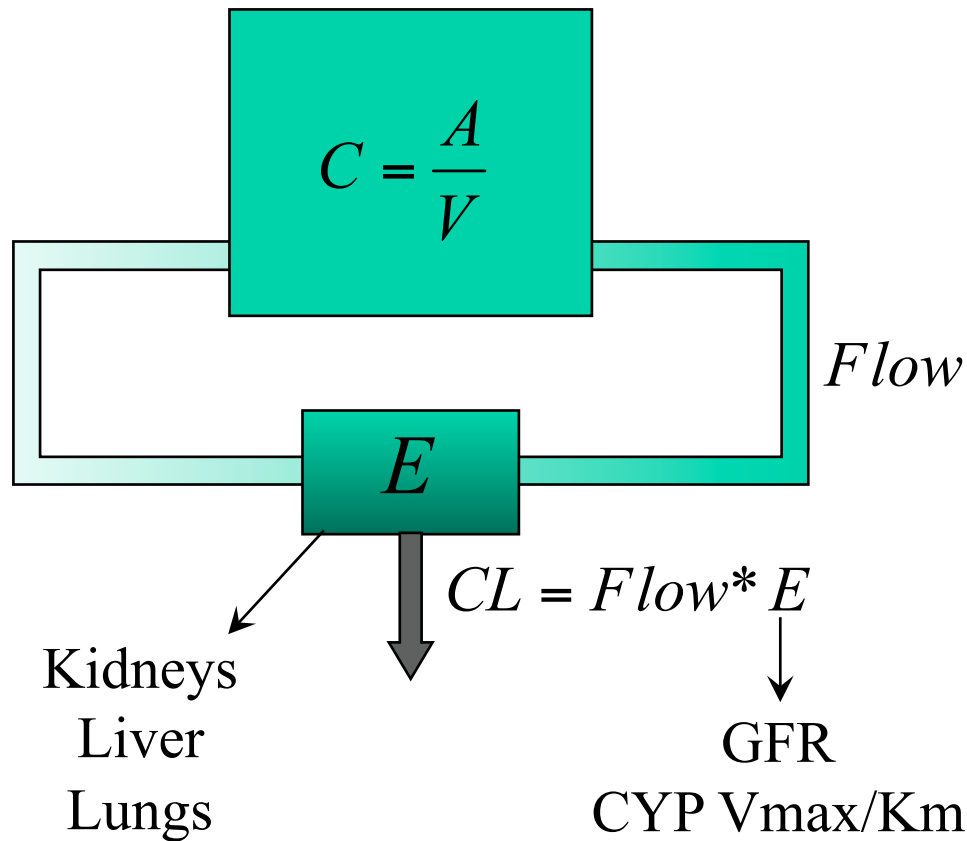
# What happens when a drug is administered as an intravenous bolus?

$$C_t = C_0 * \exp(-ke * t)$$

$$\ln(C_t) = \ln(C_0) - ke * t$$



# From 'descriptive' to 'mechanistic' model based on flow dynamic systems



$$\frac{dA}{dt} = -CL * C$$

$$\frac{dA}{dt} = -CL * \frac{A}{V}$$

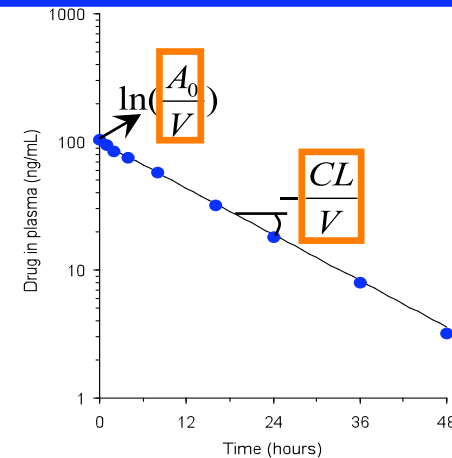
$$\frac{dA}{dt} = -\frac{CL}{V} * A$$

$$\frac{dA}{dt} = -ke * A$$

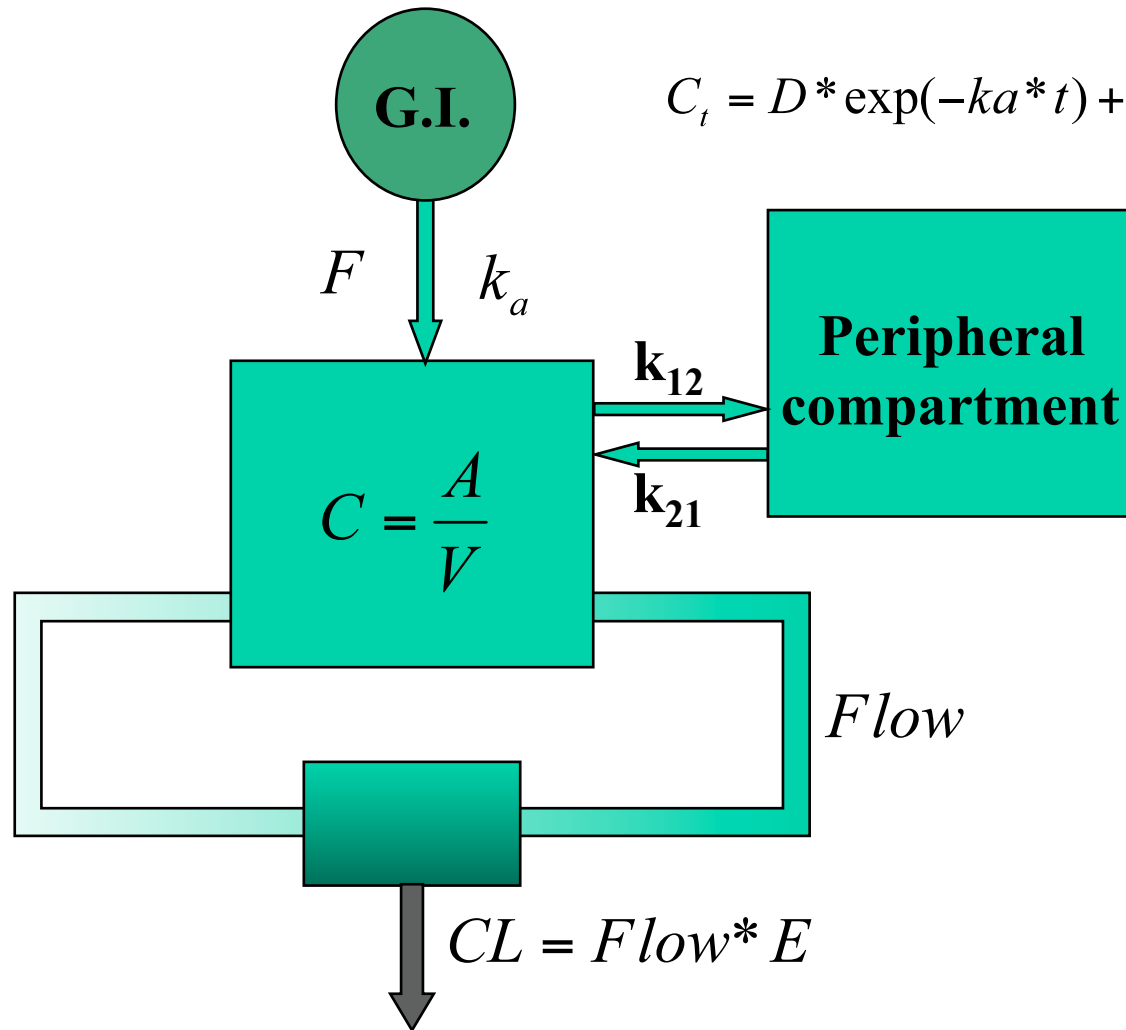
$$\frac{dC}{dt} = -ke * \frac{A}{V}$$

$$C_t = \frac{D}{V} * \exp\left(-\frac{CL}{V} * t\right)$$

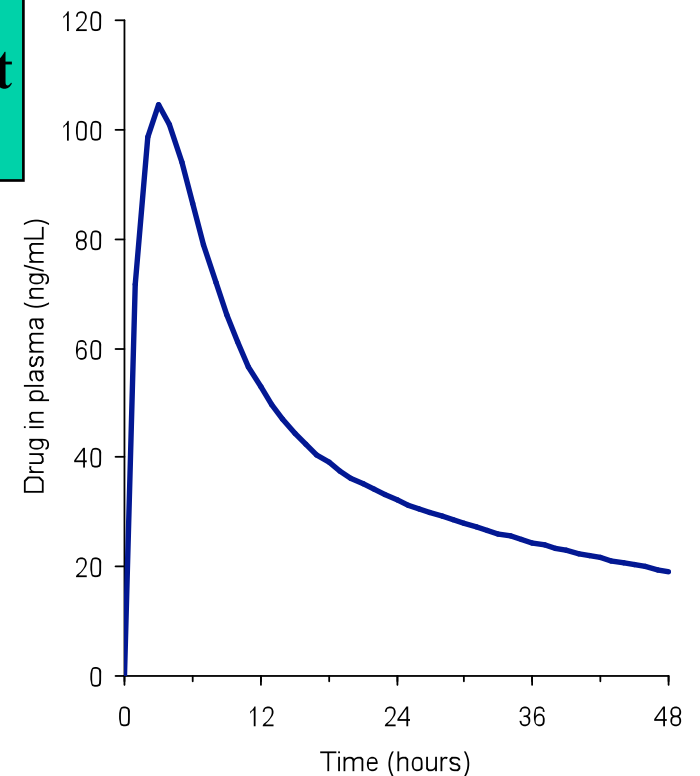
$$\ln(C_t) = \ln\left(\frac{A_0}{V}\right) - \frac{CL}{V} * t$$



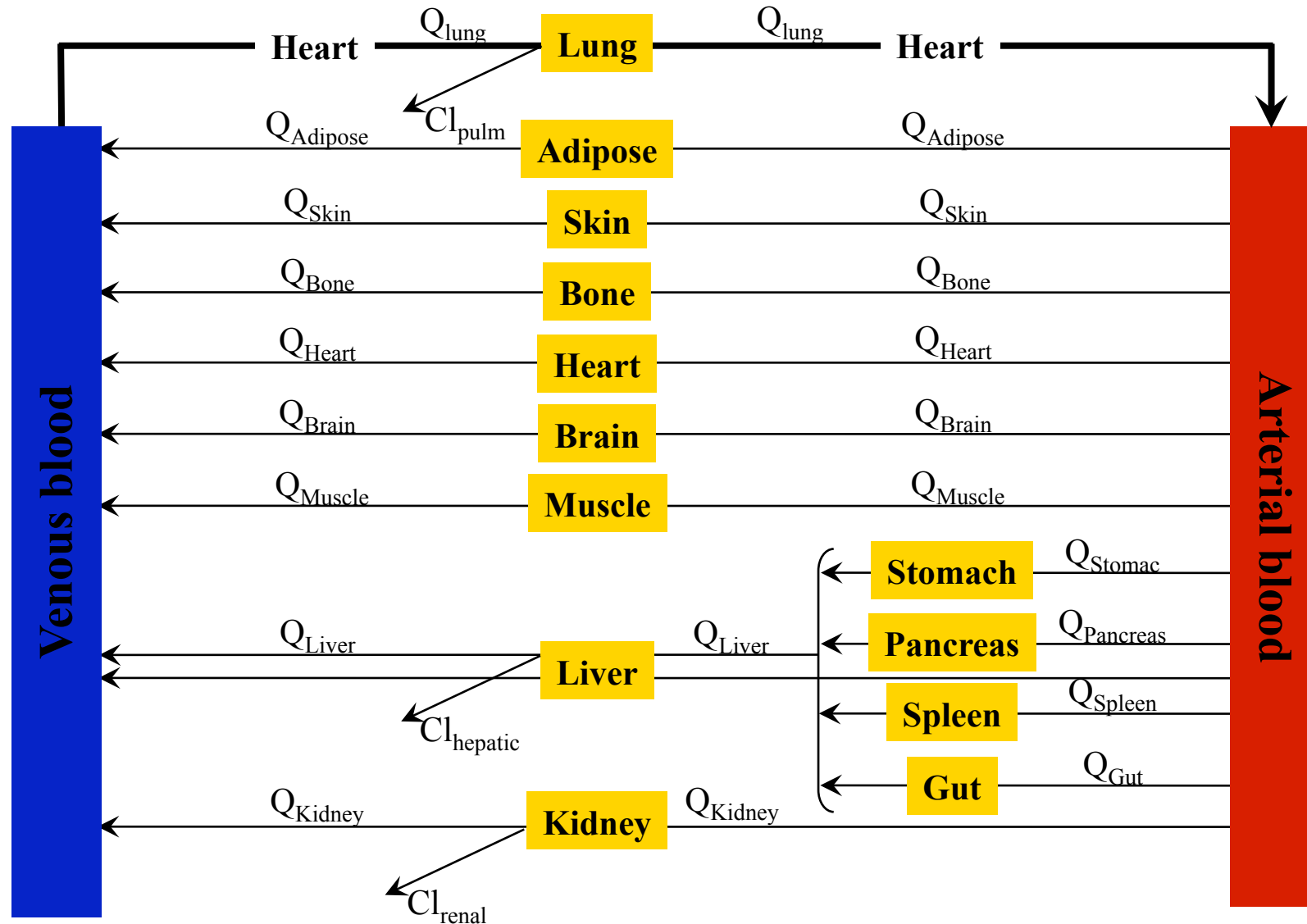
# Model with oral absorption (first order) and peripheral compartment



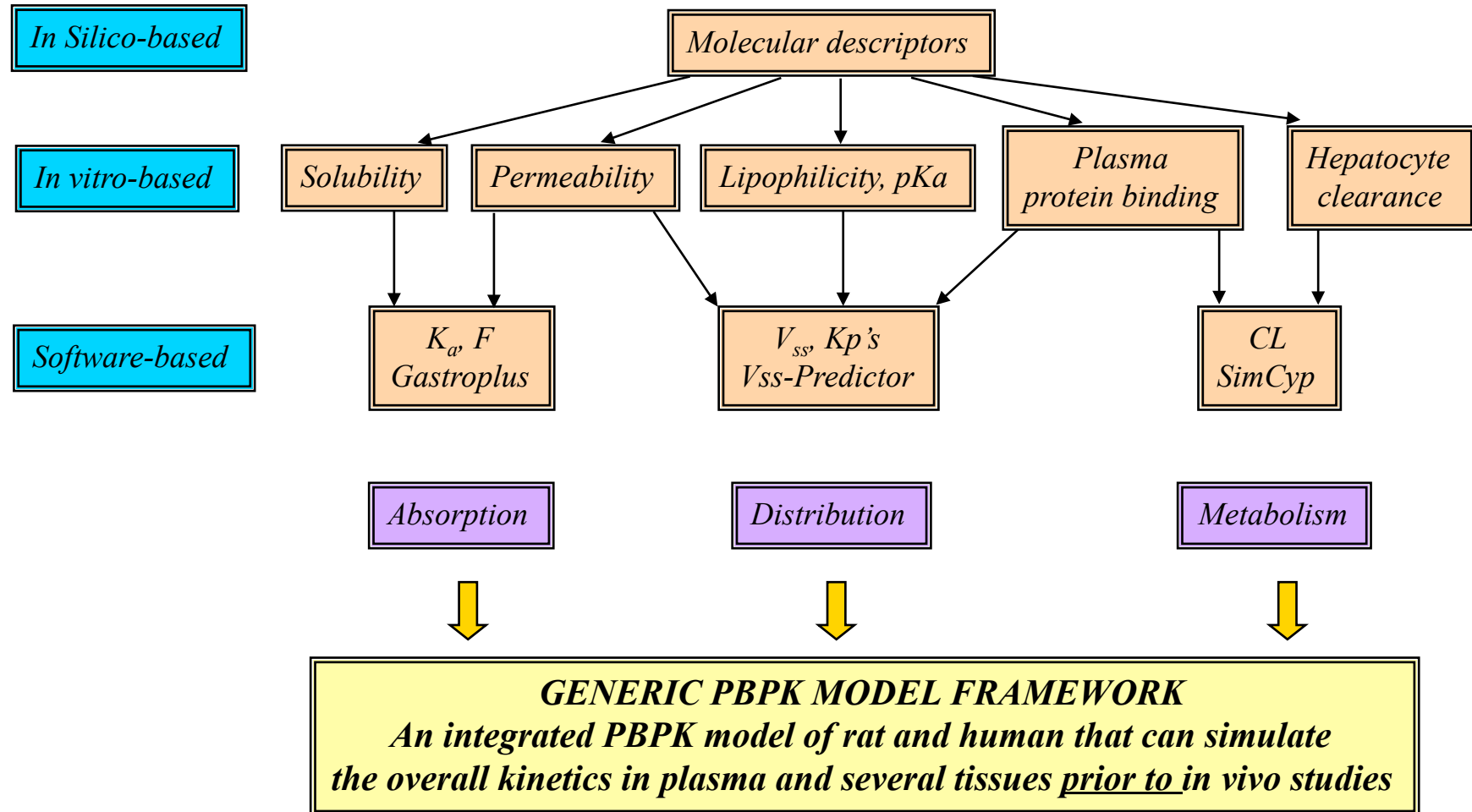
$$C_t = D * \exp(-ka * t) + A * \exp(-\alpha * t) + B * \exp(-\beta * t)$$



# Physiologically-based pharmacokinetic model (PBPK)



# From in silico to in vivo



# Pharmacodynamic models



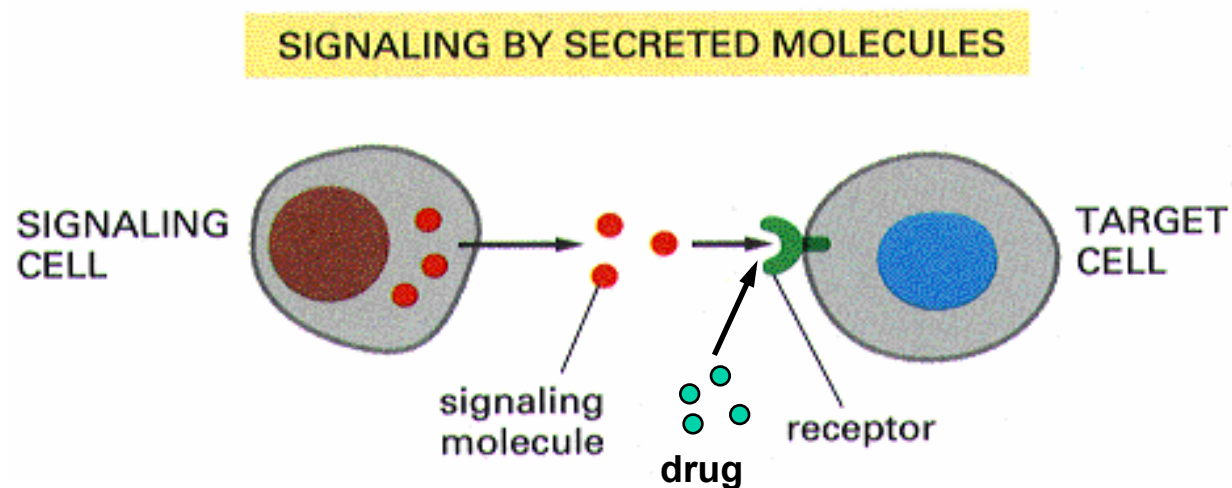
# The receptor theory

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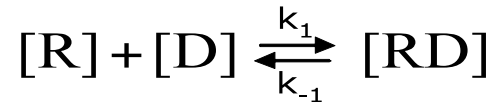
First postulated by John Langley (1820-1878)

Furthered by Paul Ehrlich (1854-1915)

“Corpora non agunt nisi fixata”



# Clark's occupation theory



$$\frac{d[RD]}{dt} = k_1 \cdot [R] \cdot [D] - k_{-1} \cdot [RD] = 0$$

$$K_D = \frac{[RT] \cdot [D]}{[RD]} - \frac{[RD] \cdot [D]}{[RD]}$$

$$k_1 \cdot [R] \cdot [D] = k_{-1} \cdot [RD]$$

$$K_D + [D] = \frac{[RT] \cdot [D]}{[RD]}$$

$$K_D = \frac{k_{-1}}{k_1} = \frac{[R] \cdot [D]}{[RD]}$$

$$[RD] = \frac{[RT] \cdot [D]}{K_D + [D]}$$

$$[RT] = [R] + [RD]$$

$$\text{Bound} = \frac{B_{MAX} \cdot \text{Free}}{K_D + \text{Free}}$$

RT or B<sub>MAX</sub> = Total amount of receptor (binding sites/mg protein or nM)

R = Free receptor (binding sites/mg protein or nM)

D or Free = Free drug (nM)

DR or Bound = complex drug-receptor (binding sites/mg protein or nM)

K<sub>1</sub> = association rate constant (min<sup>-1</sup>)

K<sub>-1</sub> = dissociation rate constant (min<sup>-1</sup>)

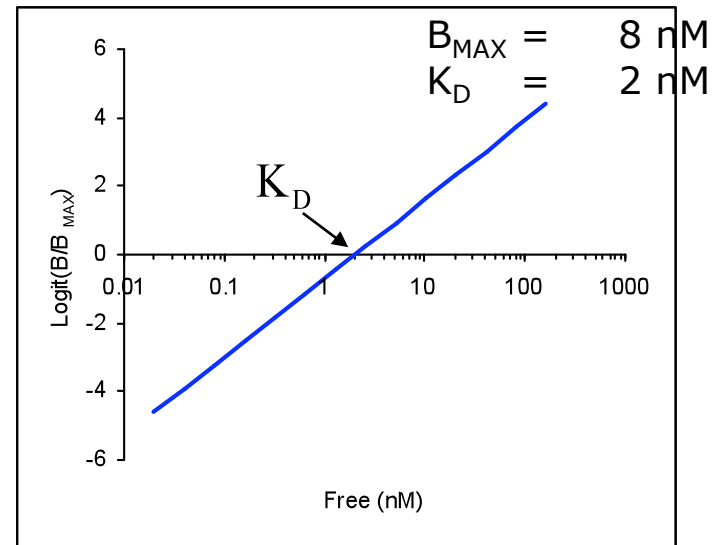
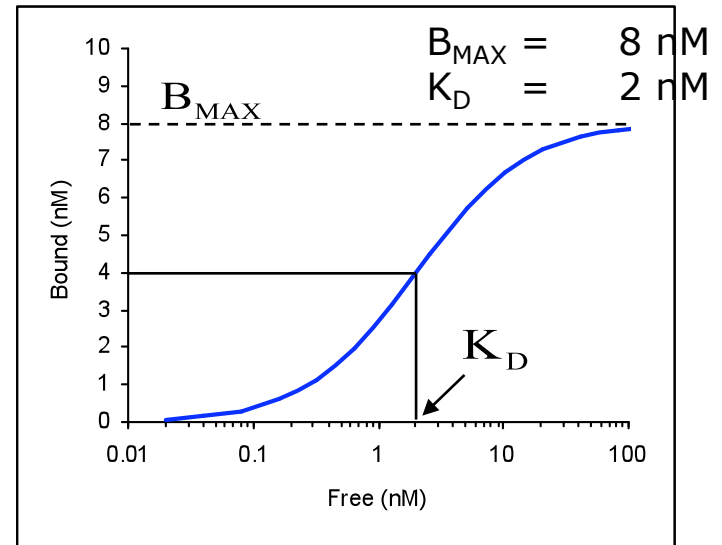
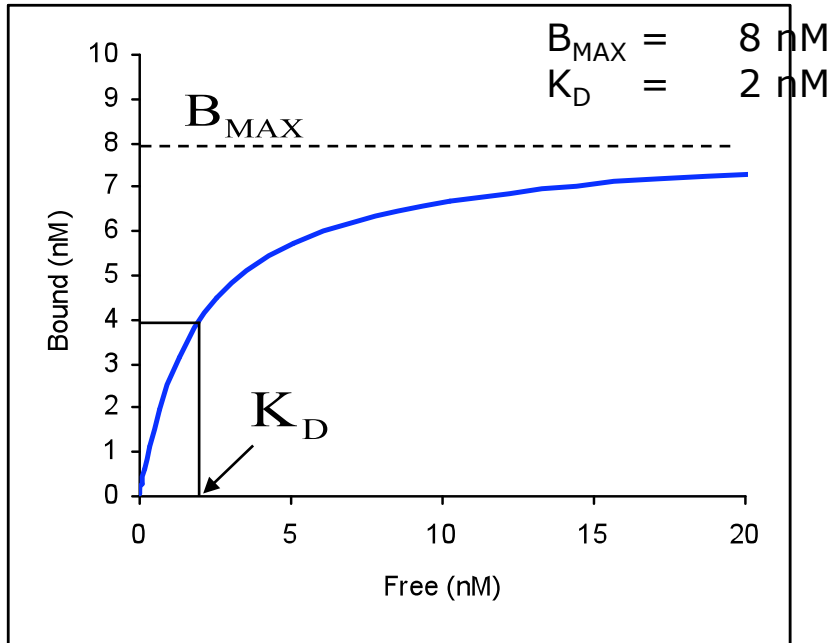
K<sub>A</sub> = Association constant

[ ] = concentration (nM)



# Some graphical representations

$$\text{Bound} = \frac{B_{\text{MAX}} \cdot \text{Free}}{K_D + \text{Free}}$$



# From receptor occupancy to pharmacological effect

## A simple view: the $E_{MAX}$ model

$$\frac{E_D}{E_{MAX}} = \frac{[RD]}{[RT]}$$

$$[RD] = \frac{[RT] \cdot [D]}{K_D + [D]}$$

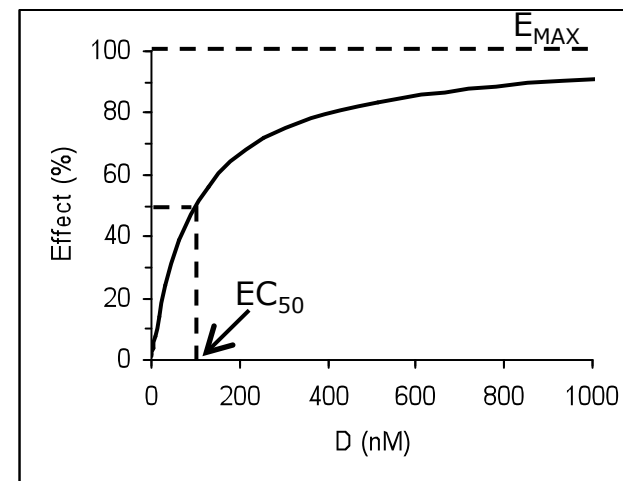
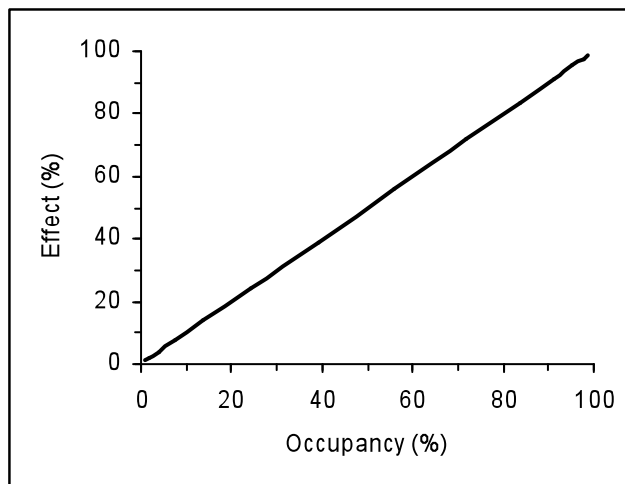
$$\frac{E_D}{E_{MAX}} = \frac{[D]}{K_D + [D]}$$

**This assumed that:**

**The measured effect was linearly related to the number of receptor occupied by the drug**

**Maximum effect was attained at maximum binding**

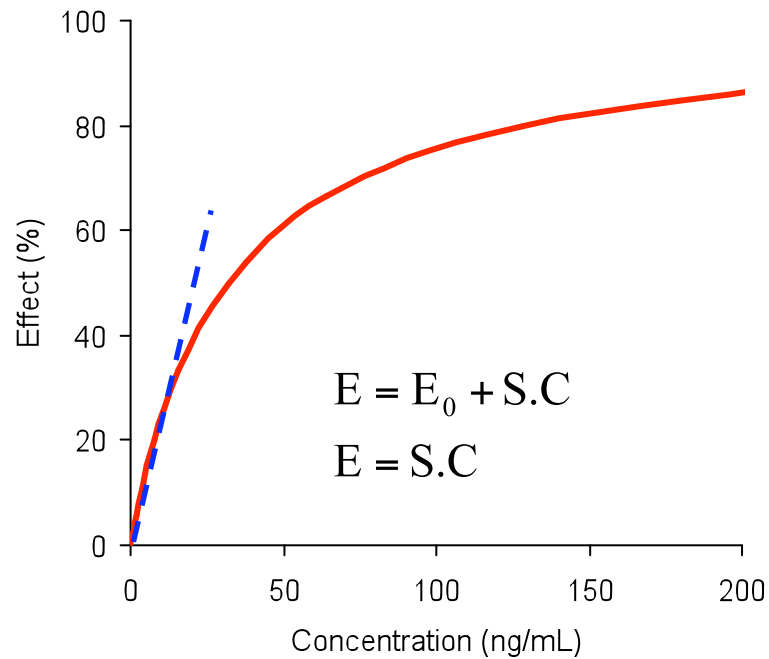
$$\text{Effect} = \frac{E_{MAX} \cdot C}{EC_{50} + C}$$



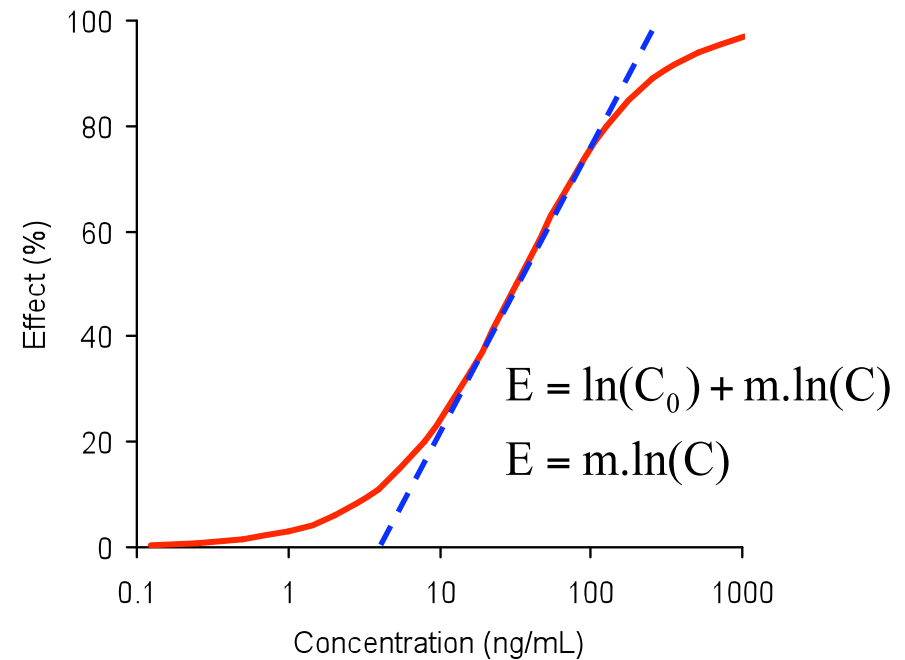
## Some derived/simplified models

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linear effect concentration model

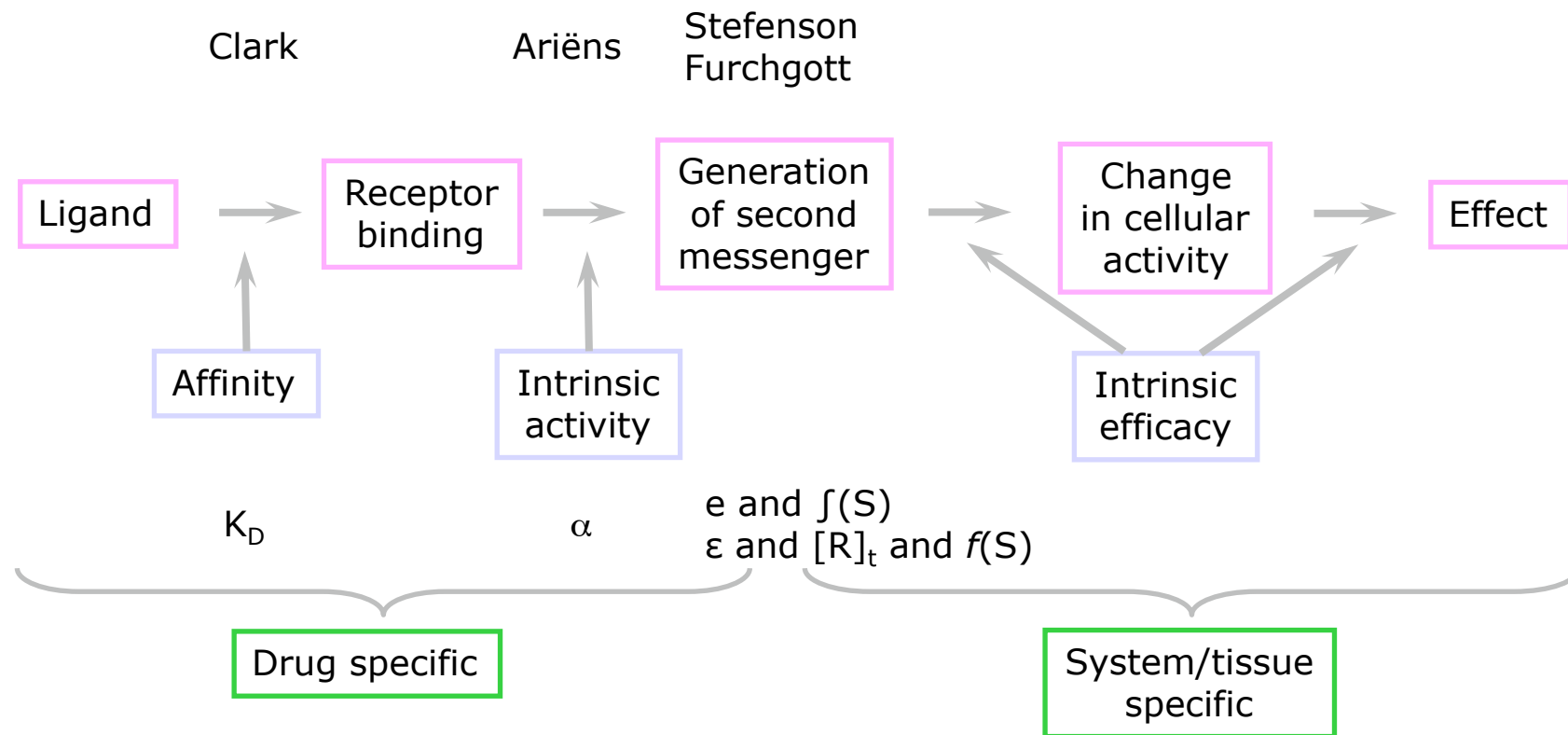


log-linear effect concentration model



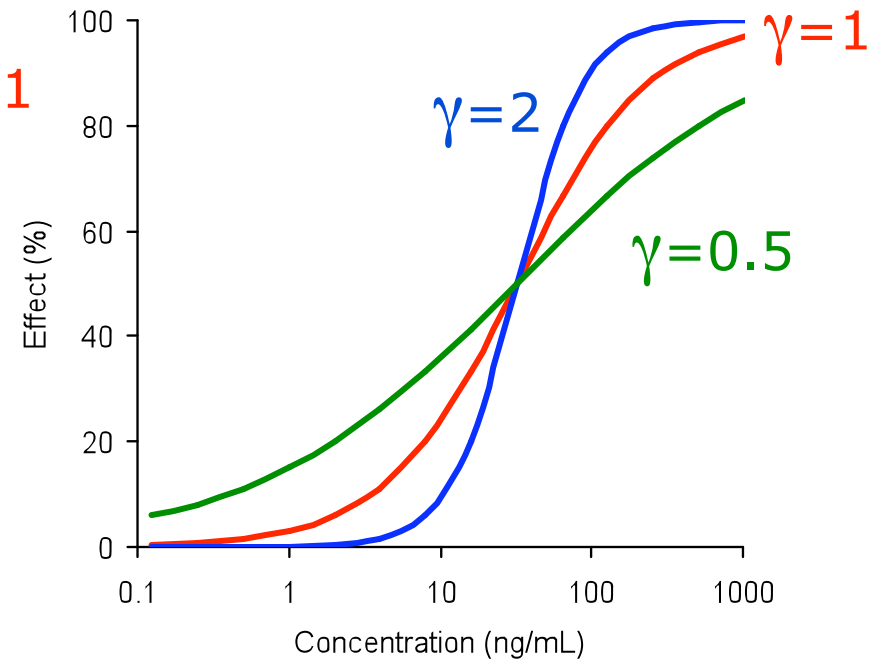
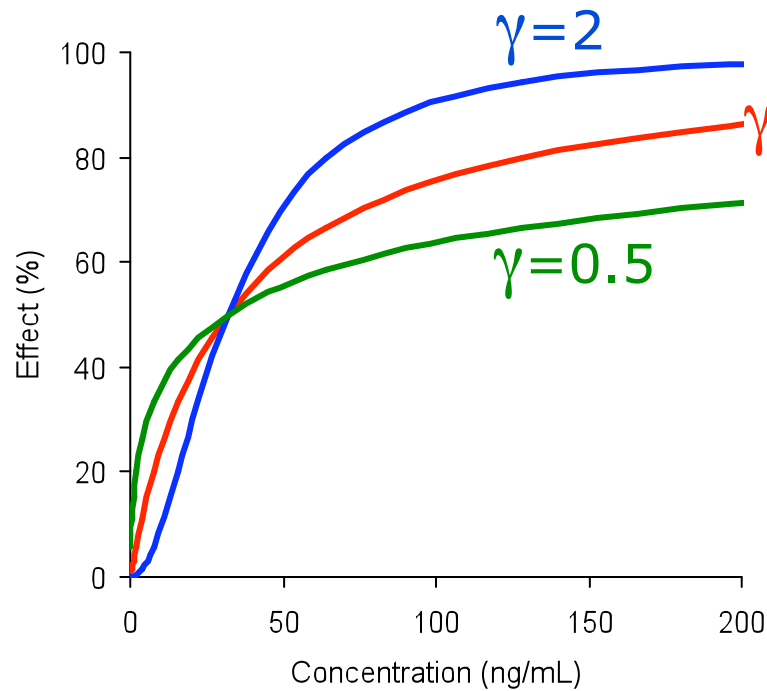
# From receptor occupancy to pharmacological effect

## A more complete view



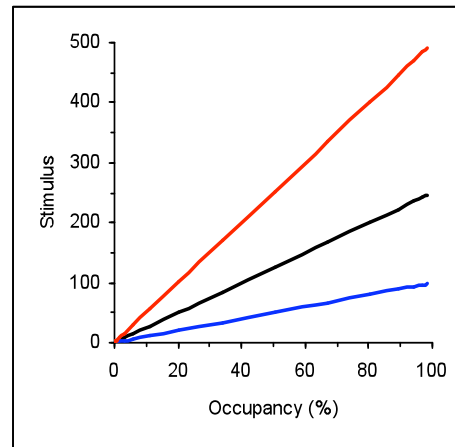
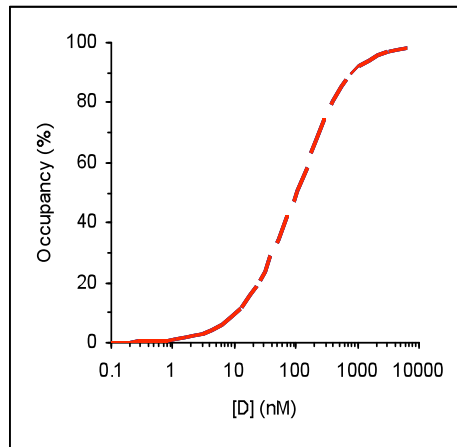
# $E_{MAX}$ model and sigmoid $E_{MAX}$ model

$$E = \frac{E_{MAX} \cdot C^\gamma}{EC_{50}^\gamma + C^\gamma}$$

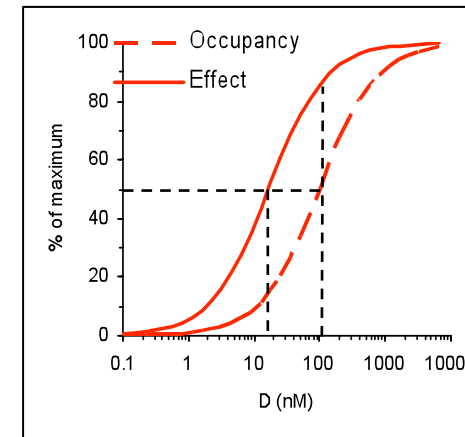
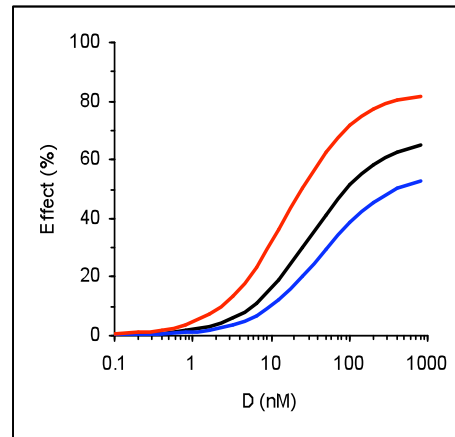
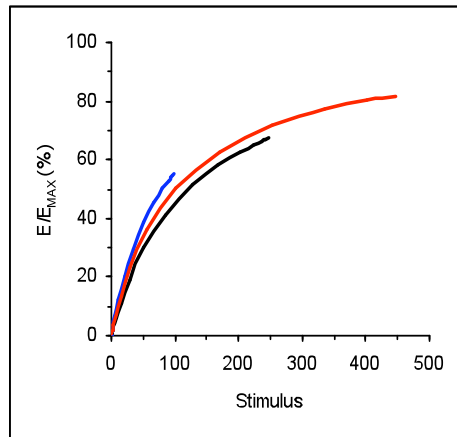


# Operational model of agonism: effect of intrinsic activity (different drugs)

$$E_D = f \left[ \frac{\varepsilon \cdot [RT]_T \cdot [D]}{[D] + K_D} \right] = f(S) \quad \text{and} \quad f(S) = \frac{S_D}{S_{50} + S_D}$$

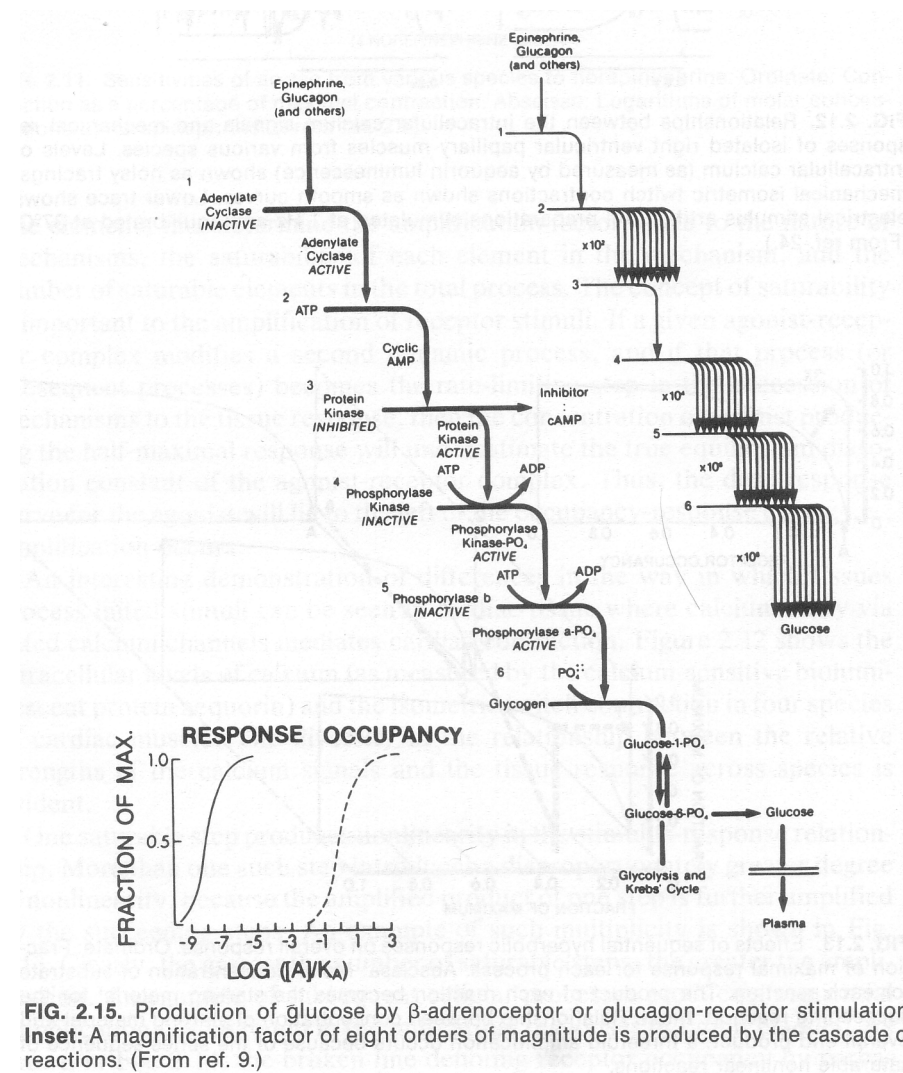


RT (nM)	KD (nM)	ε	S <sub>50</sub> (nM)
100	100	2.5	120
100	100	1	80
100	100	5	100



# Apparent dissociation between receptor occupancy and measured effect:

Production of glucose by  $\beta$ -adrenoceptor stimulation



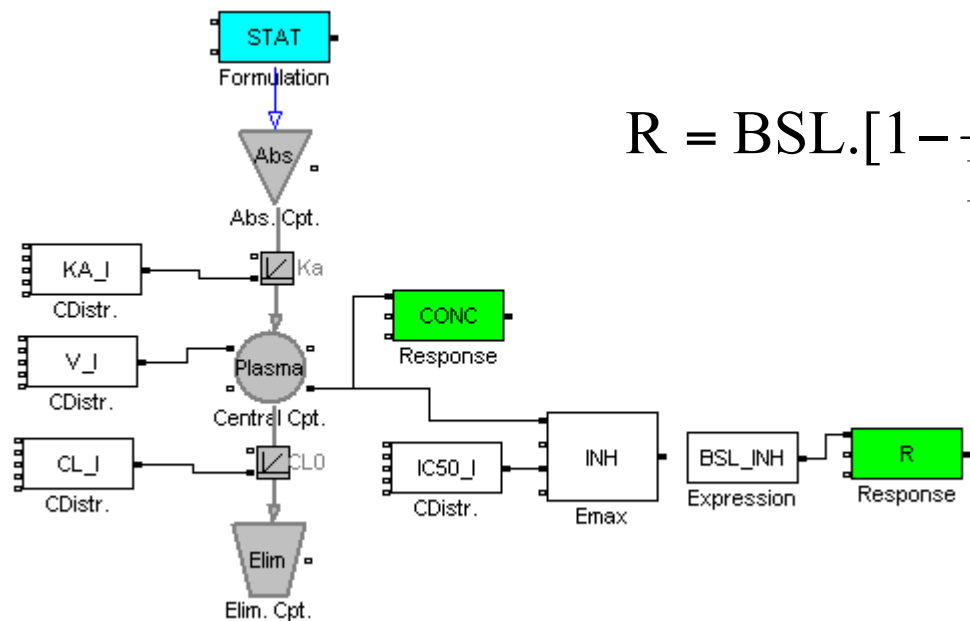
**FIG. 2.15.** Production of glucose by  $\beta$ -adrenoceptor or glucagon-receptor stimulation. **Inset:** A magnification factor of eight orders of magnitude is produced by the cascade of reactions. (From ref. 9.)

# PK-PD models



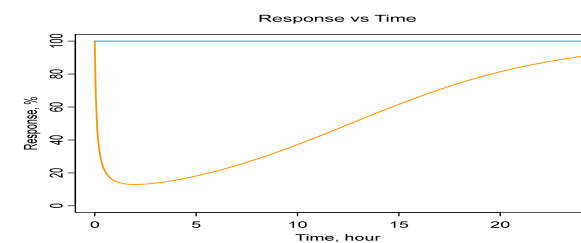
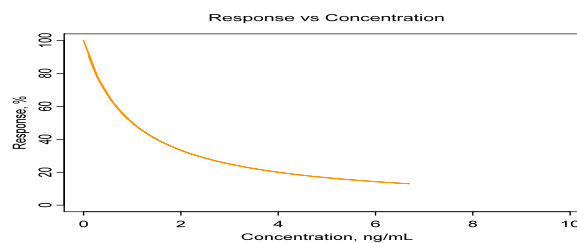
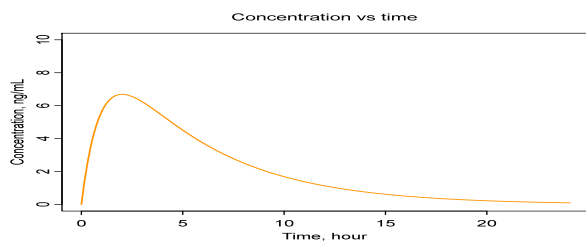


# Concentration–effect–time relationship: direct response → inhibition

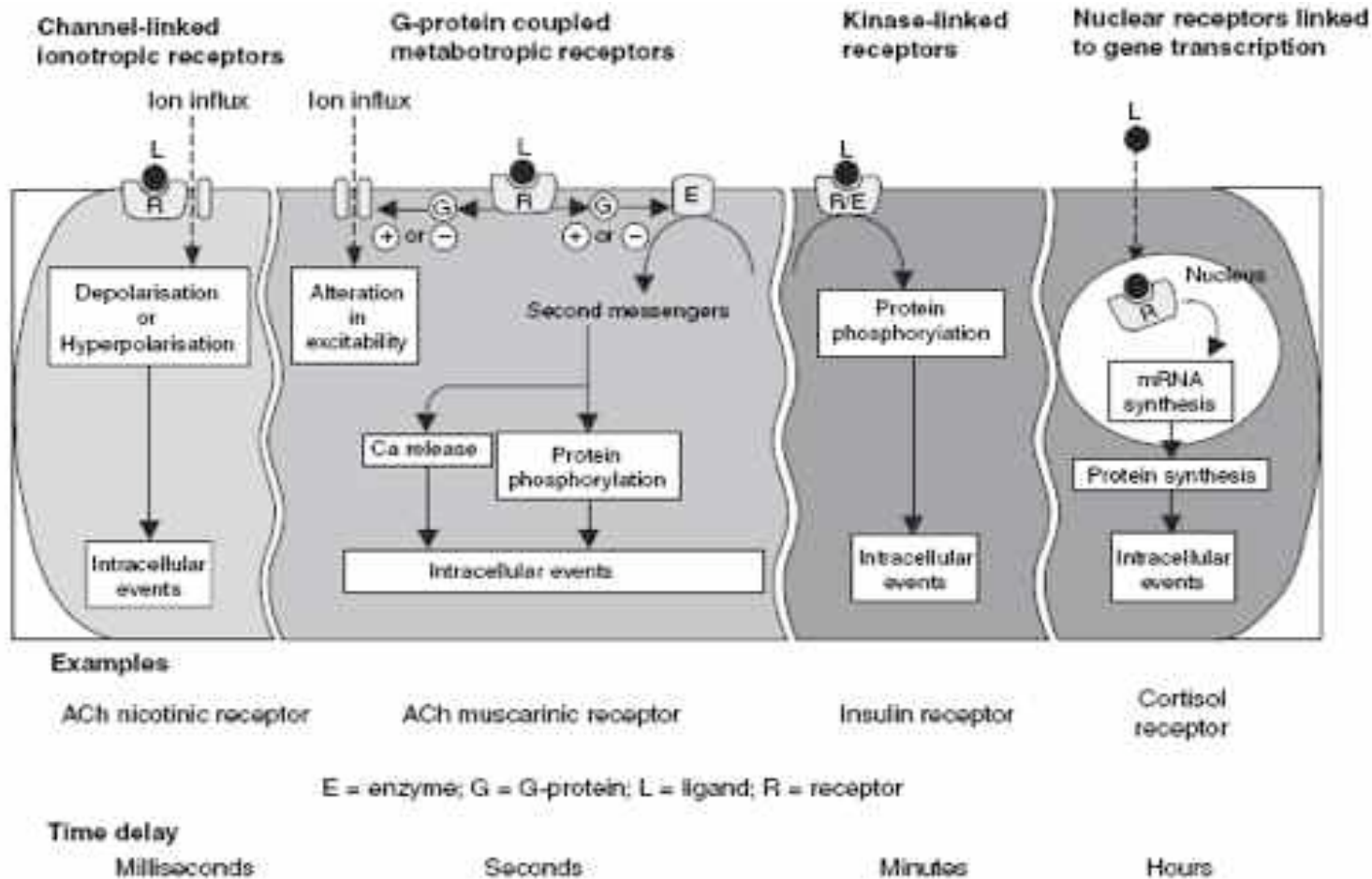


$$R = \text{BSL} \cdot \left[ 1 - \frac{I_{\max} \cdot C^n}{IC_{50}^n + C^n} \right]$$

Dose = 0.8 mg  
 KA = 1 h<sup>-1</sup>  
 V = 80 L  
 CL = 16 L.h<sup>-1</sup>  
 IC<sub>50</sub> = 1.0 ng/mL  
 n = 1.0  
 I<sub>max</sub> = 1.0  
 BSL = 100

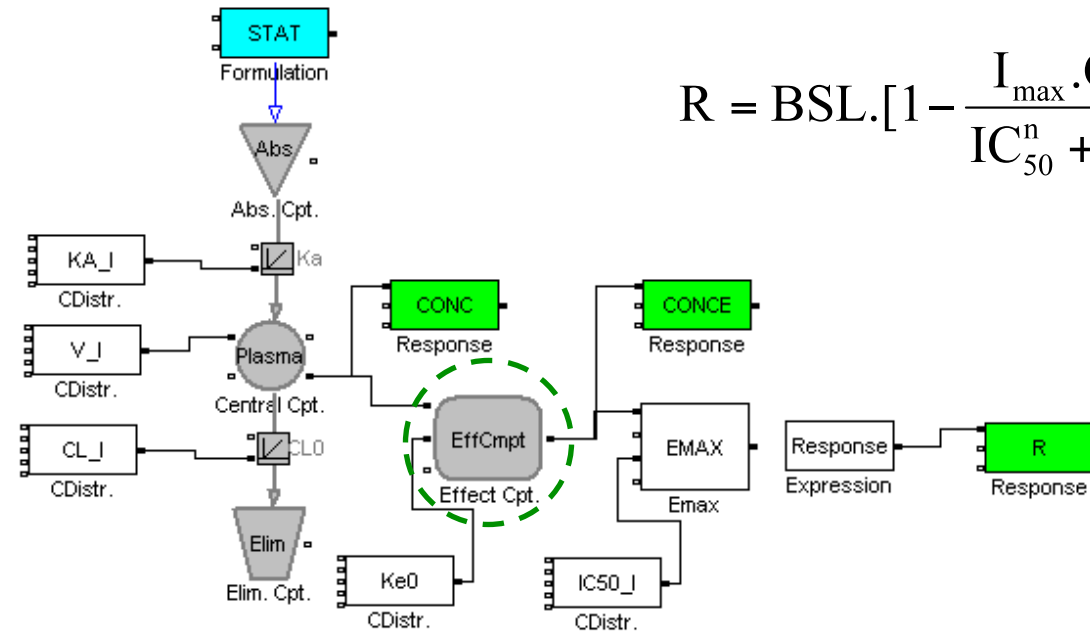


# The time delay between receptor occupancy and effect also depends on the second messenger mechanism



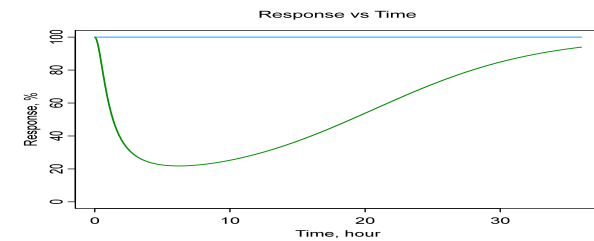
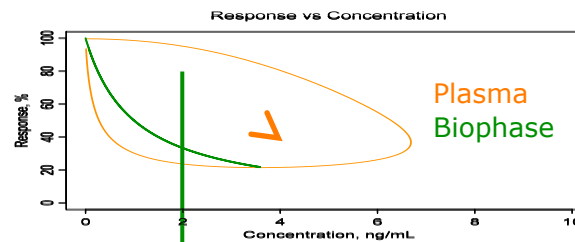
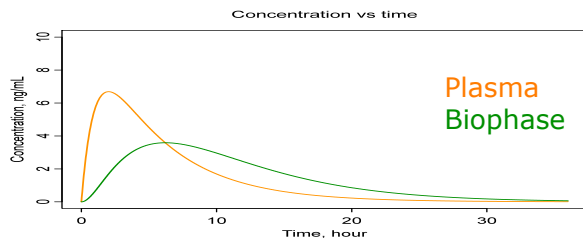
LEES, P., CUNNINGHAM, F. M. & ELLIOTT, J.  
Principles of pharmacodynamics and their applications in veterinary pharmacology.  
*Journal of Veterinary Pharmacology & Therapeutics* 27 (6), 397-414.

# Effect compartment (or Link) model



$$R = BSL \cdot \left[ 1 - \frac{I_{max} \cdot C_e^n}{IC_{50}^n + C_e^n} \right]$$

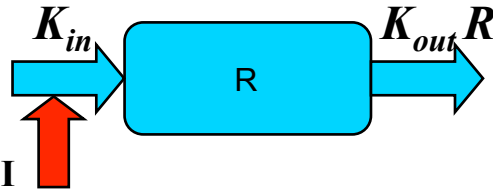
- Dose = 0.8 mg
- KA = 1 h<sup>-1</sup>
- V = 80 L
- CL = 16 L.h<sup>-1</sup>
- IC<sub>50</sub> = 1.0 ng/mL
- n = 1.0
- I<sub>max</sub> = 1.0
- BSL = 100
- Ke0 = 0.2 h<sup>-1</sup>



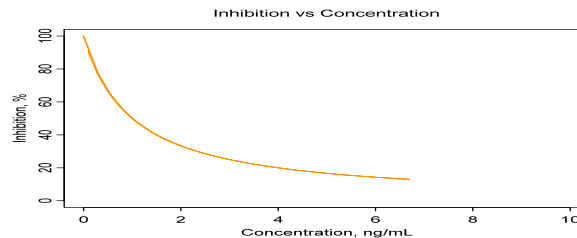
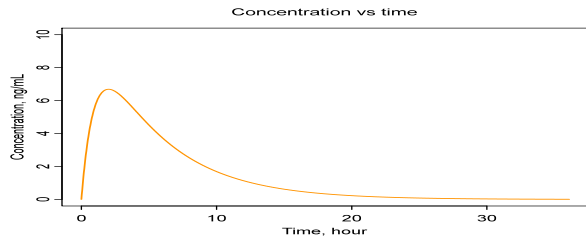
Biophase

# Concentration–effect–time relationship for an indirect response model with inhibition of build-up

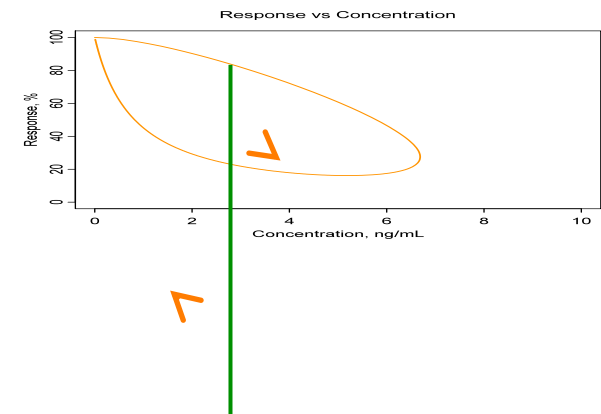
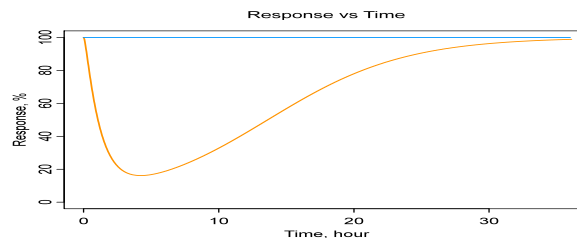
Inhibition of build-up :



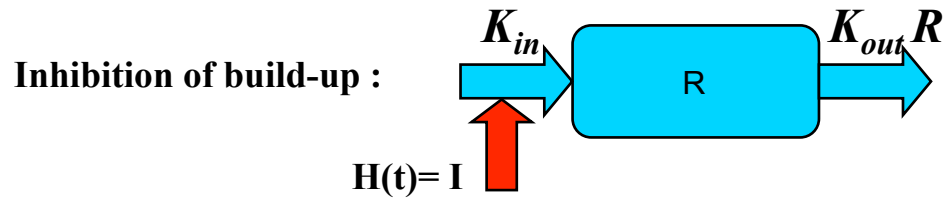
$$\frac{dR}{dt} = k_{in} \cdot \left[ 1 - \frac{I_{max} \cdot C^n}{IC_{50}^n + C^n} \right] - K_{out} \cdot R$$



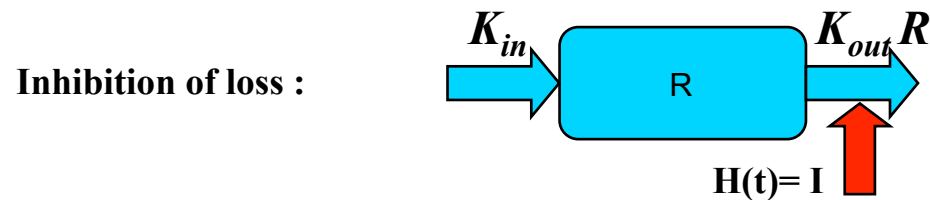
- Dose = 0.8 mg
- KA = 1 h<sup>-1</sup>
- V = 80 L
- CL = 16 L.h<sup>-1</sup>
- IC<sub>50</sub> = 1.0 ng/mL
- n = 1.0
- I<sub>max</sub> = 1.0
- K<sub>in</sub> = 100 Runits.h<sup>-1</sup>
- K<sub>out</sub> = 1 h<sup>-1</sup>



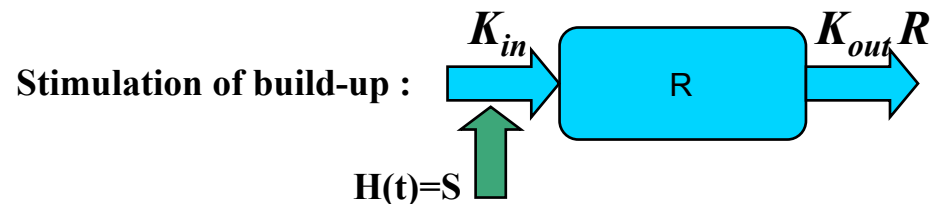
# Indirect response models



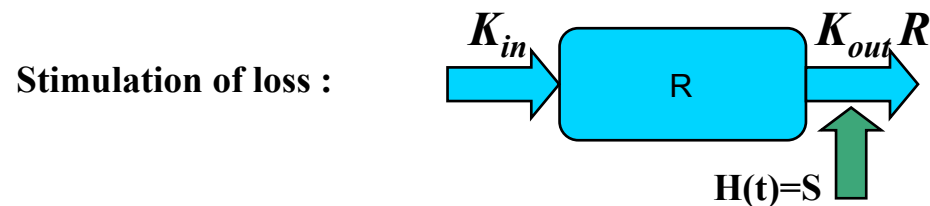
$$\frac{dR}{dt} = k_{in} \cdot \left[ 1 - \frac{I_{max} \cdot C^n}{IC_{50}^n + C^n} \right] - K_{out} \cdot R$$



$$\frac{dR}{dt} = k_{in} - k_{out} \cdot \left[ 1 - \frac{I_{max} \cdot C^n}{IC_{50}^n + C^n} \right] \cdot R$$

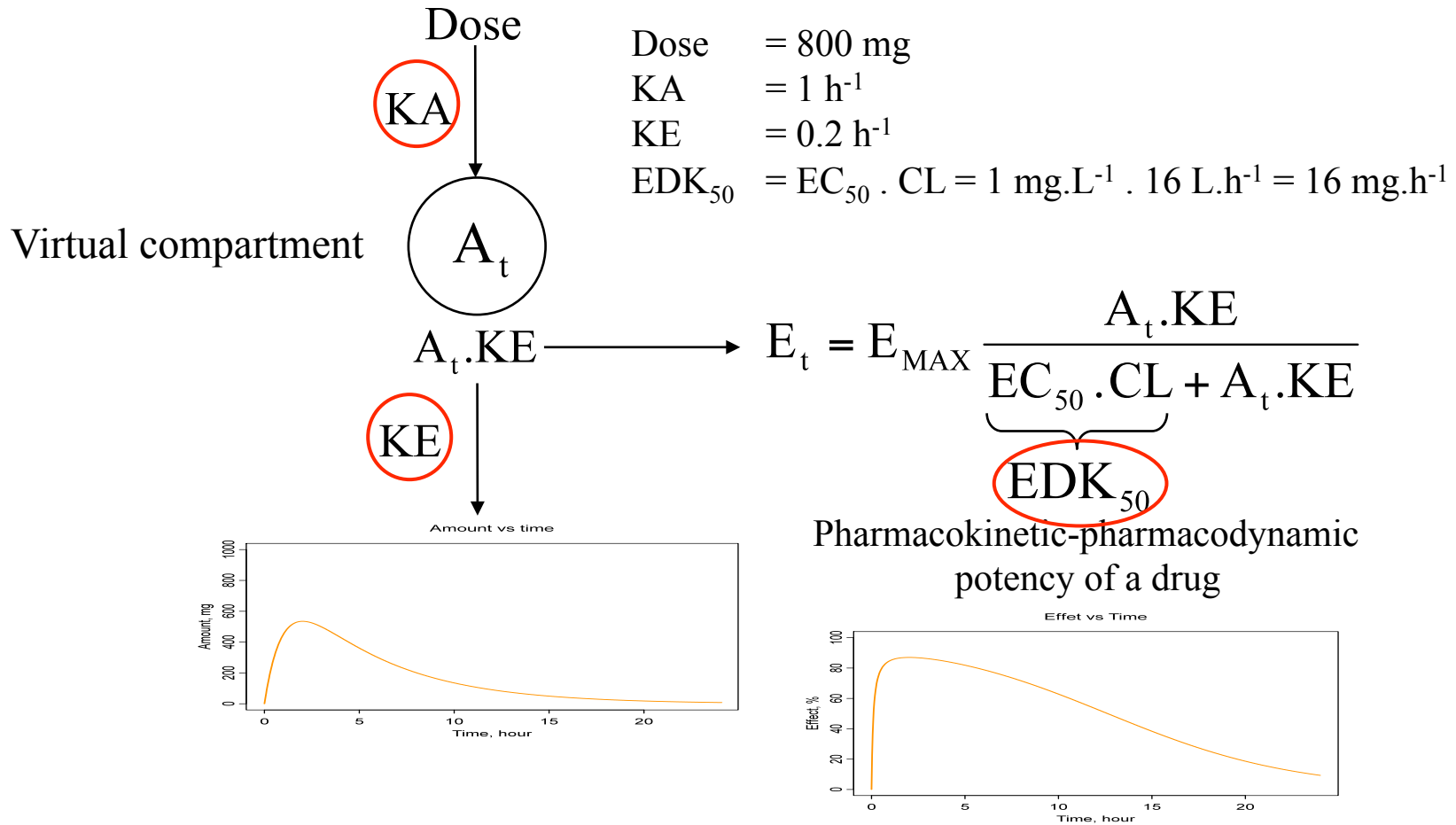


$$\frac{dR}{dt} = k_{in} \cdot \left[ 1 + \frac{E_{max} \cdot C^n}{EC_{50}^n + C^n} \right] - k_{out} \cdot R$$



$$\frac{dR}{dt} = k_{in} - k_{out} \cdot \left[ 1 + \frac{E_{max} \cdot C^n}{EC_{50}^n + C^n} \right] \cdot R$$

# KPD model: analysis of effect-time profile in the absence of pharmacokinetic data



# Mechanistic model: example of a viral kinetic model based on the predator-prey principle (Lotka-Volterra)

Target cell (activated CD4+ cells):

$$dT/dt = b - d_1 \cdot T - (1-**INH**) \cdot i \cdot V \cdot T$$

Actively infected cells (short-lived):

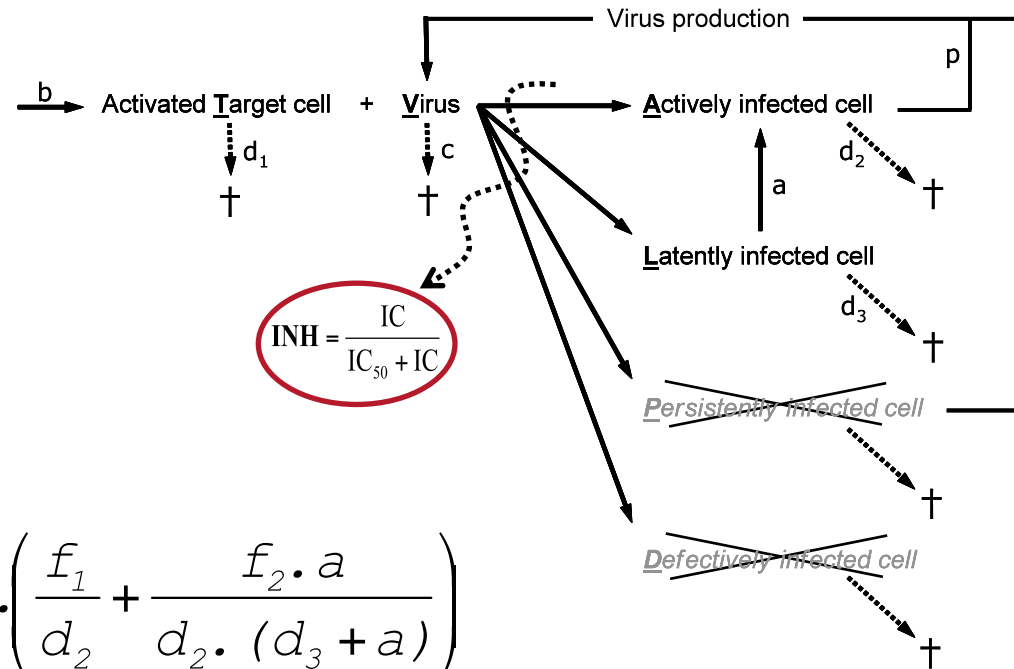
$$dA/dt = f_1 \cdot (1-**INH**) \cdot i \cdot V \cdot T - d_2 \cdot A + a \cdot L$$

Latently infected resting cells (long lived):

$$dL/dt = f_2 \cdot (1-**INH**) \cdot i \cdot V \cdot T - d_3 \cdot L - a \cdot L$$

Infectious virus (copies HIV-1 RNA):

$$dV/dt = p \cdot A - C \cdot V$$



$$RR0 = \frac{b}{d_1} \cdot i \cdot \frac{p}{c} \cdot \left( \frac{f_1}{d_2} + \frac{f_2 \cdot a}{d_2 \cdot (d_3 + a)} \right)$$

$$RR0_{INH} = (1 - INH) \cdot RR0$$

$RR0_{INH} > 1 \rightarrow$  growth  
 $RR0_{INH} = 1 \rightarrow$  survival  
 $RR0_{INH} < 1 \rightarrow$  extinction

$$RMIC = (RR0 - 1) \cdot IC_{50}$$

*Pre-clinical application:*

*Modelling the anti-lipolytic effect of an  
adenosine A<sub>1</sub>-receptor agonist*

The data were obtained from:

E.A Van Schaick, H.J.M.M. De Greef, M.W.E. Langemeijer, M.J. Sheehan, A.P. IJzerman,  
and M. Danhof,;

Pharmacokinetic-pharmacodynamic modeling of the anti-lipolytic and anti-ketotic effects of  
the adenosine A<sub>1</sub>-receptor agonist N<sup>6</sup>-(p-sulphophenyl)adenosine in rats.

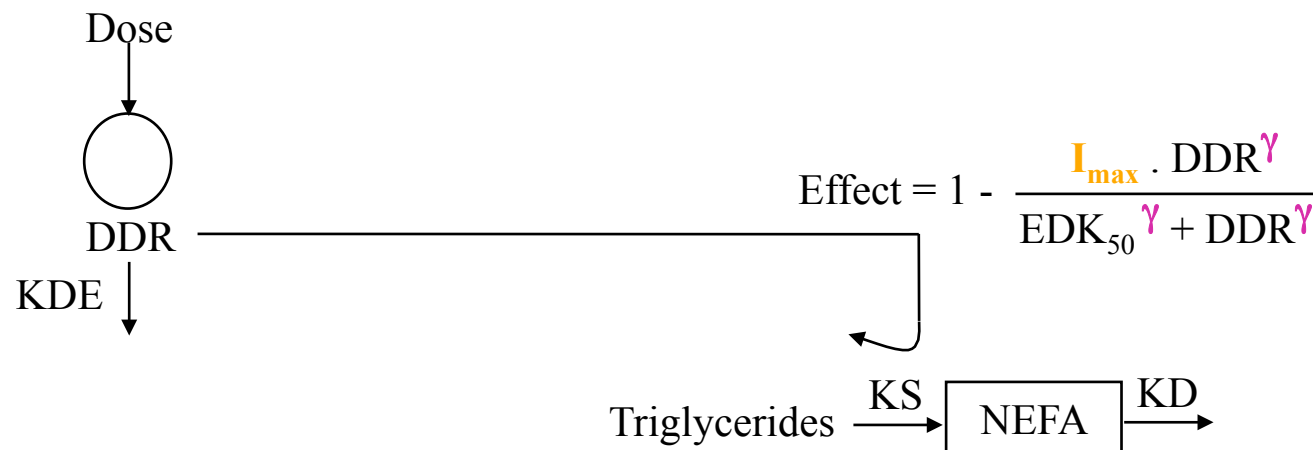
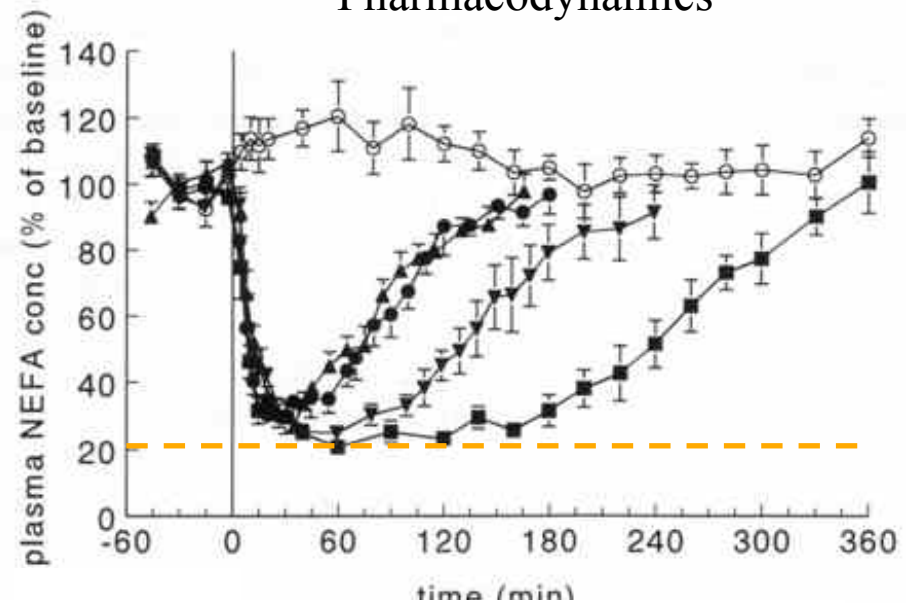
*Br. J. Pharmacol.*, **122**, 525-533 (1997)



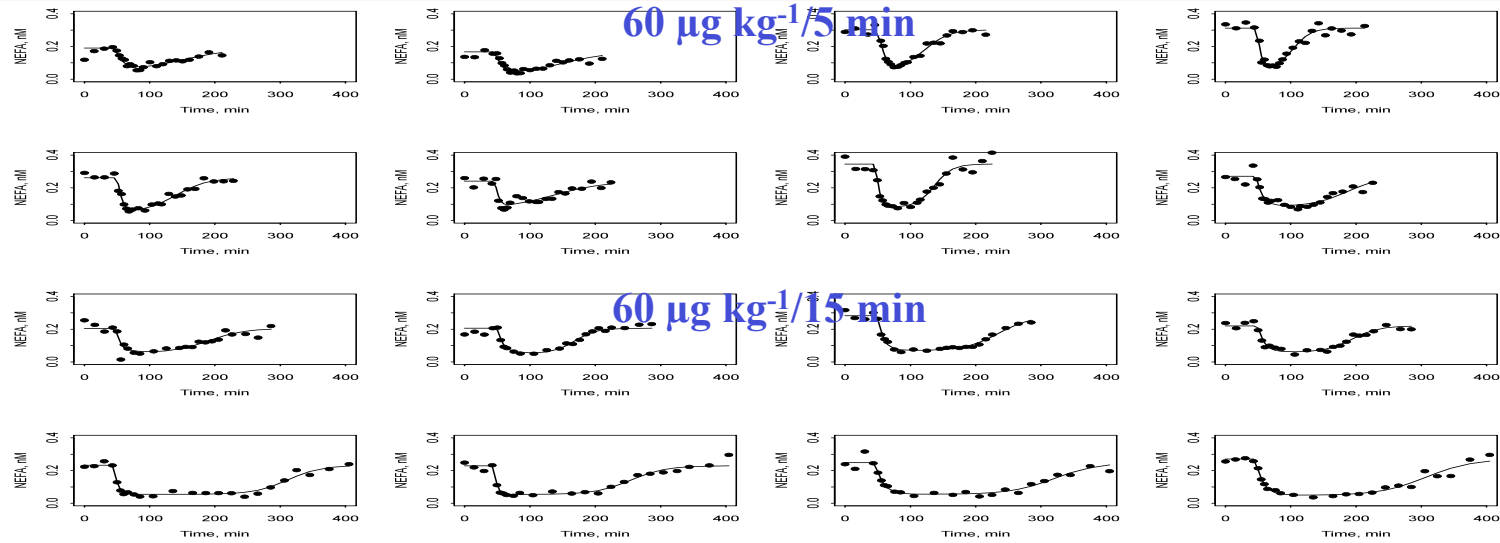


# Would it be possible to analyse the dose-response-time data in absence of pharmacokinetics?

Pharmacodynamics



# The individual NEFA plasma concentration-time profiles are fitted well with an adapted K-PD model



The parameters  $EDK_{50}$ ,  $\beta/KDE$ ,  $E_{max}$ ,  $\gamma$  and baseline are similar

*Differences in  $KD/K_{out}$  usually occur when the effect is directly linked to the central compartment and the compound follows a multi-compartmental distribution*

PK-PD			K-PD		
Parameters	Mean	SE	Parameters	Mean	SE
(Pharmaco)kinetics					
Cl (ml.min <sup>-1</sup> )	2.3	± 0.1			
$\beta$ (min <sup>-1</sup> )	<b>0.018</b>	± <b>0.001</b>	KDE (min <sup>-1</sup> )	<b>0.020</b>	± <b>0.002</b>
Pharmacodynamics					
$K_{in}^*$ (nM.mL <sup>-1</sup> .min <sup>-1</sup> )	<b>0.026</b>	± <b>0.003</b>	KS (nM.mL <sup>-1</sup> .min <sup>-1</sup> )	<b>0.046</b>	± <b>0.005</b>
$K_{out}$ (min <sup>-1</sup> )	<b>0.105</b>	± <b>0.009</b>	KD (min <sup>-1</sup> )	<b>0.165</b>	± <b>0.01</b>
BSL (nM)	<b>0.26</b>	± <b>0.01</b>	BSL* (nM)	<b>0.28</b>	± <b>0.03</b>
IC <sub>50</sub> (ng.mL <sup>-1</sup> )	<b>22.4</b>	± <b>1.8</b>			
EDK <sub>50</sub> * (µg min <sup>-1</sup> )	<b>0.050</b>	± <b>0.003</b>	EDK <sub>50</sub> (µg min <sup>-1</sup> )	<b>0.056</b>	± <b>0.004</b>
I <sub>max</sub> ** (fraction of BSL)	<b>0.80</b>	± <b>0.01</b>	I <sub>max</sub> (fraction of BSL)	<b>0.77</b>	± <b>0.01</b>
$\gamma$	<b>2.2</b>	± <b>0.2</b>	$\gamma$	<b>2.1</b>	± <b>0.1</b>

\* Secondary parameters

\*\* I<sub>max</sub> was fixed for the 15 µg in 5 min and 15 µg in 15 min treatments

# Simulation



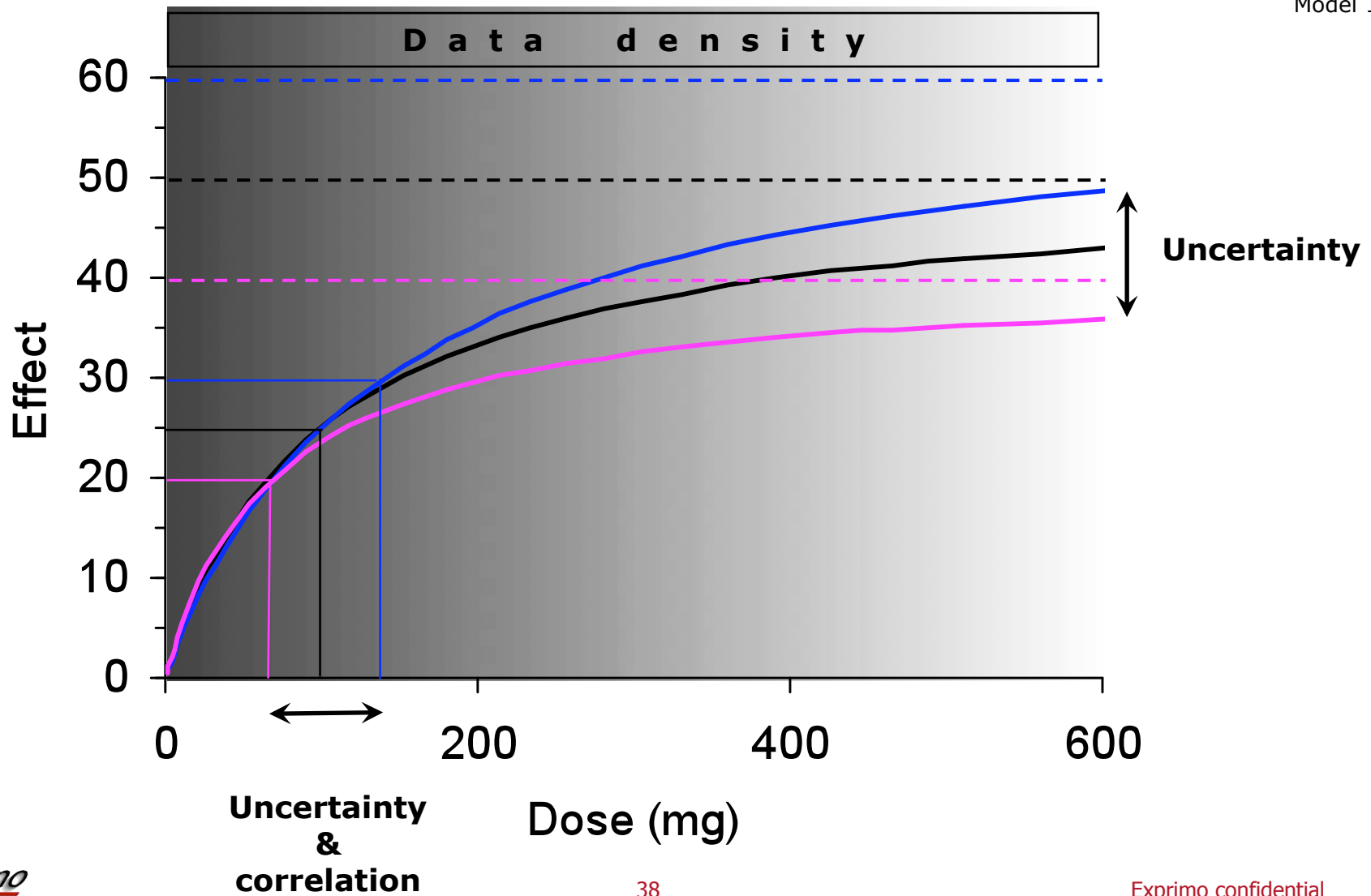
# Some principles (1)

---

- Simulation models usually consist of
  - Structural model equations
  - Structural model parameters
    - Mean
    - Uncertainty
    - Correlation between parameter estimates
  - Random parameters
    - inter-individual variability
    - intra-individual variability
    - inter-occasion variability
- Simulations are usually performed at different levels
  - Typical subject
  - Entire (sub-)population
  - Study

# Uncertainty and correlation of parameter estimates

Model 18

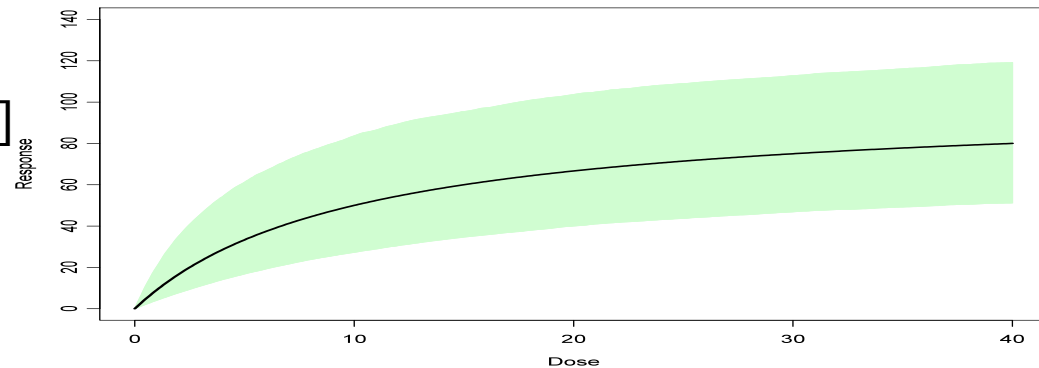


# Simulations excluding correlation between the parameters

---

## *Model*

- $E_{\max}$  dose-response model
- $ED_{50}$  (mean [CV])= 10 mg [60%]
- $E_{\max}$  (mean [CV])= 100 [30%]
- Correlation not implemented



## *Simulations*

- 1500 replicates

## *Results*

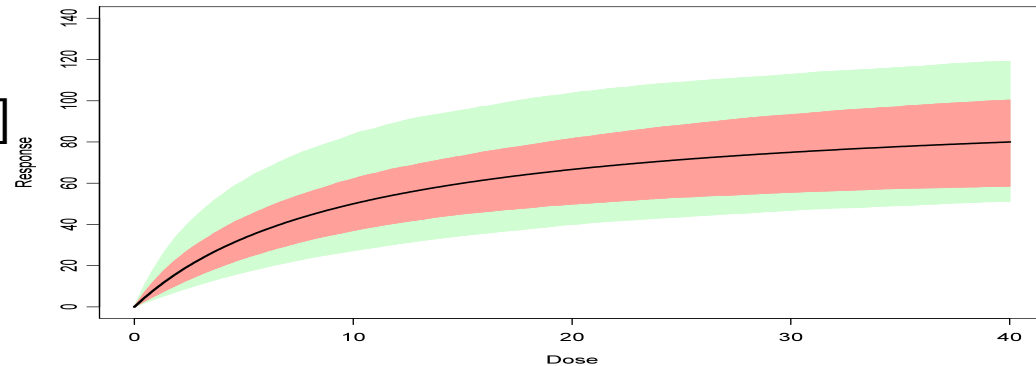
- 10, 50 and 90 percentiles of response in function of dose

# Simulations including correlation between the parameters

---

## Model

- $E_{\max}$  dose-response model
- $ED_{50}$  (mean [CV])= 10 mg [60%]
- $E_{\max}$  (mean [CV])= 100 [30%]
- Correlation implemented = 0.8



## Simulations

- 1500 replicates

## Results

- 10, 50 and 90 percentiles of response in function of dose

Desired effect



## Some principles (2)

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- Simulations can be performed to:
  - Describe observations
  - Explain observations
  - Understand the system
  - Interpolate and/or extrapolate
  - Estimate the risks associated to
    - Random effect
    - Uncertainty
    - Hypothesis
  - Evaluate different (if) scenarios or hypotheses
  - Optimize study designs
  - Others...

## Conclusion/recommendation

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**Magritte 1929**

# Backup slides



# Analysis of the PK-PD data



## Parameterization: ensure that sampled parameters are meaningful and simulations realistic

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- Estimate transformed parameters
  - e.g. estimating  $\log(\text{ED}_{50})$  will ensure values of  $\text{ED}_{50} > 0$  when sampling from uncertainty

$$R = \frac{E_{\text{MAX}} \cdot \text{Dose}}{e^{\log \text{ED}_{50}} + \text{Dose}}$$

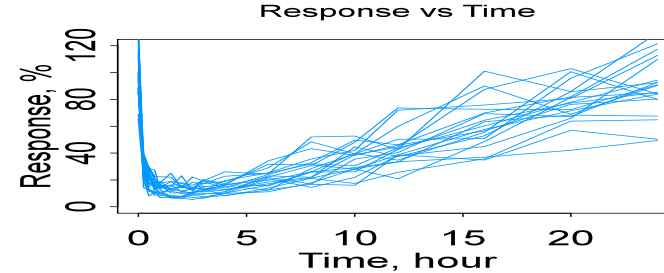
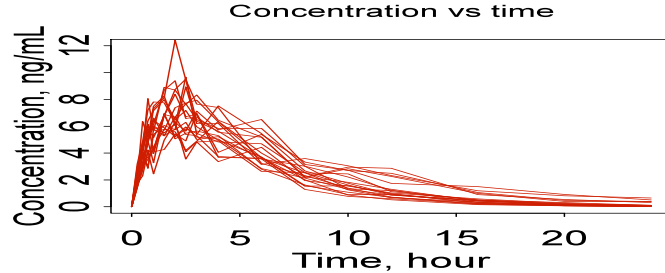
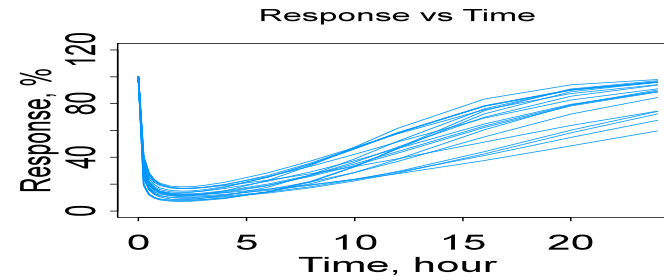
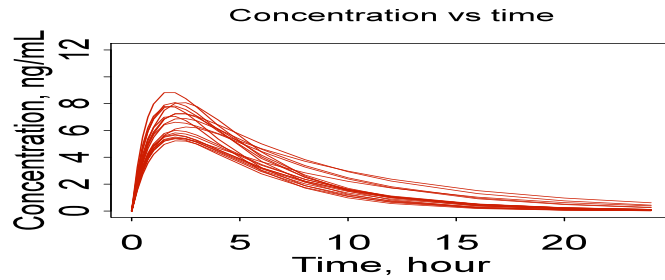
- Assume log-normal distribution when acceptable

$$P_{1i} = \text{THETA}_1 * \exp(\eta_{1i}) \text{ or } P_{1i} = \log(\text{THETA}_1) + \eta_{1i}$$

- If response needs to be between 0 and 1, use logit transformation
- Evaluate the correlation in the parameter estimates and in the inter-subject random effect

Non-linear (mixed effect) modelling is recommended to estimate the fixed (mean) and random (inter-individual and residual variability) parameters of PK-PD models

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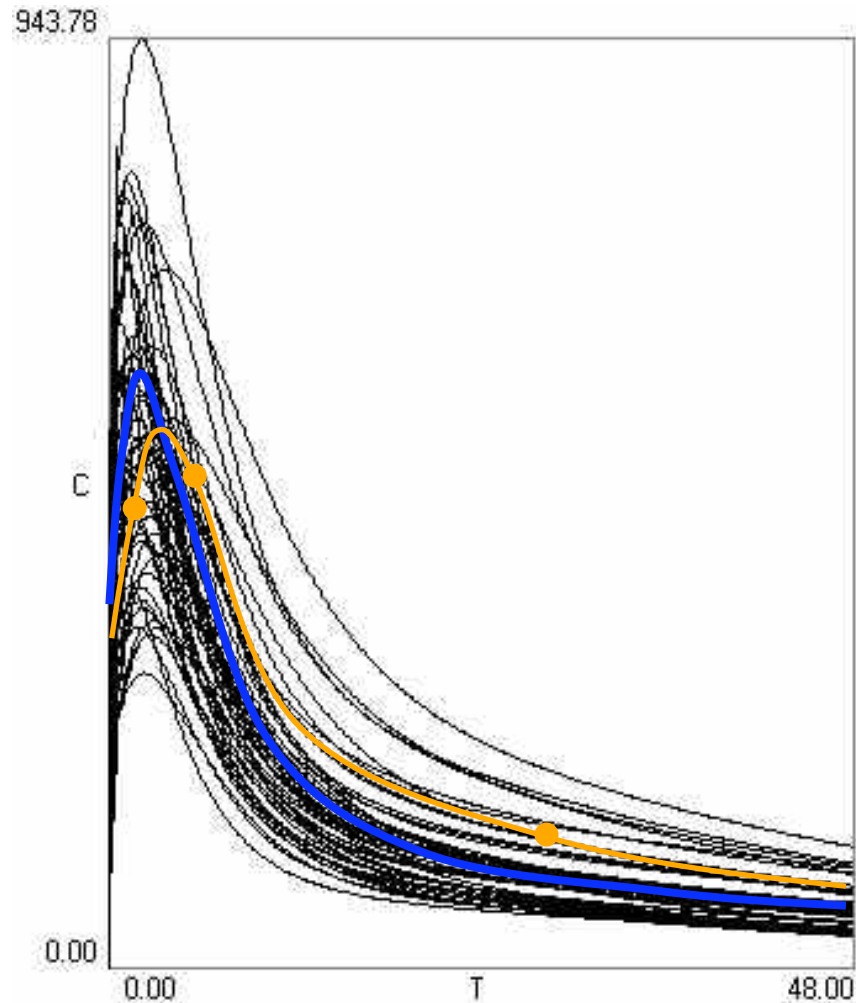
Empirical Bayesian Estimation is used to estimate the individual model parameters (e.g. POSTHOC function of NONMEM)

$$SS = \sum_{i=1}^n \frac{(C'_p - C_p)^2}{\delta^2} + \sum_{j=1}^m \frac{(P'_j - P_j)^2}{\omega_j^2}$$

Where:

- m = number of parameters
- n = number of data points
- Cp' = predicted serum level
- Cp = observed serum level
- $\delta$  = standard deviation of drug assay
- P' = revised population parameter
- P = population parameter
- $\omega$  = standard deviation of population parameter

<http://www.rxkinetics.com/bayes.html>



## Available software for modeling in PK-PD

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- NONMEM
- MONOLIX
- WinNonlin, WinNonMix
- SAS
  - PROC NLIN
  - PROC MIXED
- S-PLUS
  - lm, lmList
  - nls, nlminb
  - lme, nlme, etc



# Available software for simulation in PK-PD

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- NONMEM
- MONOLIX
- WinNonlin, WinNonMix
- SAS
- S-Plus
- MATLAB
- Pharsight Trial Simulator (TS2)
- Berkeley Madonna
- ACSL
- Adapt
- Stella
- P-Pharm
- Pspice
- Mathematica
- And many others ...